

RULES IN RELATIONAL CONTRACTS*

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ABSTRACT. We present a novel explanation of why organizations become more bureaucratic over time in spite of their efforts to foster worker initiative. Worker initiative in adapting to local information ensures efficiency but requires strong incentives. When incentives are relational and the firm faces shocks that erode its credibility, the firm may adopt rules that ignore local information but yield satisfactory (though suboptimal) performance. Rules help the relationship survive the current shocks, but inflict inefficiencies in the future. While the relationship may recover, its ability to weather future shocks deteriorates, and, over time, it becomes more reliant on rules.

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1. INTRODUCTION

Management scholars and practitioners alike routinely promote the virtues of worker empowerment. An empowered worker can generate large benefits for the firm by taking initiative and adapting his actions to local information that the top management need not be aware of. “Empowerment in many ways is the reverse of doing things by the book” (Zemke and Schaaf, 1989, p. 68), and in order to encourage their workers to take initiative, firms often keep their work rules vague with little or no stipulations on how the workers should perform their jobs.

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Nordstrom, a leading departmental store chain based in the United States, offers a classic example of such lack of rules. For years, Nordstrom's employee handbook simply stated "Our number one goal is to provide outstanding customer service. Set both your personal and professional goals high [...]" Nordstrom Rules: Rule #1: Use good judgment in all situations. There will be no additional rules" (Spector and McCarthy, 2012).

However, it is not uncommon for organizations to get mired in bureaucracy as new rules get added over time. Even the firms that insist on worker initiative as a key to their success go through phases where emphasis on discretion gives way to rule-based work. In particular, during a time of crisis a typical response of the top management is to centralize operations by removing discretions given to the lower-ranking employees, and implementing new rules that standardize the work process and clarify which job aspects the workers should focus on (Slatter and Lovett, 1999).

The implementation of rules presents a natural trade-off. Rules compromise production efficiency as they ignore local information. But, it may be easier to incentivize rule-based work than to encourage worker initiative; the workers may find it less onerous to follow a standardized work process than to acquire local information and use their judgment to act accordingly. The adoption of new rules, however, has another critical implication: rules may convey information on what job aspects are weighed more heavily by the organization and what compromises are acceptable (Cyert and March, 1963). And such information leakage aggravates the incentive problem in the future. When the workers are again asked to take initiative and exert consummate effort, they may perpetuate inefficiency by taking the cheaper rule-based action instead (Williamson, 1999).

March et al (2000; pp. 45–47) presents a case study of Stanford University that offers an example of such information implications of new rules. Until 1970s, the university maintained that tenure should be granted to the faculty member who is "best available" and "most accomplished" in his or her field. Competency in scholarly research, teaching, and service were all deemed important but the precise meaning of these tenure criteria were left unspecified. However, following several contentious cases of tenure denials in the 1970s, the university implemented a more formal rule that clarified the weights to be given on the different aspects of a faculty member's job. It was stated that "both scholarship and teaching are important prerequisites for tenure," but "service, however exemplary, cannot substitute for deficiencies in scholarship or teaching."

In this article we study how the information implications of new rules affect the dynamics of worker initiative in a long-term employment relationship. We explore when worker initiative should be encouraged, when it should give way to standardized work rules, and what the

implications of adopting standardized rules are for the relationship's future. Our findings suggest that while rules can help the relationship survive in times of crisis, they may critically undermine the value of the on-going relationship. Once the rules are implemented, it becomes harder to foster worker initiative in the future; the organization becomes more fragile to future shocks, and tends to rely on the rules more frequently.

The example of Hewlett-Packard Company speaks to our key findings. Hewlett-Packard, from its inception through early 1980s, was known for its highly decentralized structure ("The HP Way") where divisions were highly autonomous and employees were strongly encouraged to take initiative on actions that advanced the firm's goals. But in the 1980s, the company found itself in turmoil and, in response, adopted a more centralized mode of operation. Nevertheless, within a decade HP again decentralized its operations, but its decentralized structure did not persist for long. In subsequent years, the company continued to return to centralization frequently as it oscillated between the two organizational modes (Nickerson and Zenger, 2002; House and Price, 2009).¹

We formalize this argument by using a model of relational contract between a firm and a liquidity-constrained worker.² In every period, the worker privately takes an action in order to perform his job. Production efficiency requires the worker to adapt his action to the underlying circumstances so as to guarantee a high output. However, the firm can also put in place a standardized work process that can yield high output with some probability even if the worker ignores the underlying state of the world and simply follow the rules. Such a "rigid" action (i.e., doing things as per the rules) is less costly to the worker than the efficient "adaptive" one. Moreover, once the rigid action is made available, the worker can always use it in the future, even when the costly adaptive action is called for (this assumption captures the idea that new rules convey information on what compromises in the production process are acceptable to the firm). The firm promises the worker a discretionary bonus tied to his performance as a relational contract. But, in every period, the firm may privately face a liquidity shock and fail to pay the worker due to a lack of funds. The dynamics of the optimal contract stems from such exogenous shocks as they erode the firm's credibility, and, consequently, its ability to offer relational incentives.

¹In reality, the oscillation between rules-based work and emphasis on worker initiative is typically embedded in a broader swing between centralization and decentralization (Bartlett and Ghoshal, 1998).

²When local information and worker initiative are critical for production, verifiable measures of performance may be elusive. Therefore, incentives may be provided through relational contracts where the firm's credibility depends on the future surplus generated in the relationship (Levin, 2003; also see Malcomson, 2012, for a survey).

We show that the optimal relational contract exhibits a dynamics that goes through three distinct phases. At the beginning of the relationship, the firm incentivizes the worker to take initiative and the worker chooses the adaptive action, as the future surplus is large and the firm's credibility is high. Moreover, the firm earns the maximum feasible payoff by appropriating all rents. However, if there is a liquidity shock, the firm cannot pay the worker and is forced to renege on its promise. Since the shock is privately observed by the firm, the worker must punish the firm when it fails to pay, and the firm is required to transfer some of the future surplus to the worker. As a result, the firm's stake in the relationship is reduced and its credibility depletes. If the shocks are not too severe, the firm continues to encourage worker initiative. Once the shock passes and the firm makes good on its promise, the relationship recovers completely: the players' payoffs immediately revert back to what they were at the beginning of the relationship.

However, if there are too many consecutive shocks, the firm faces a significant loss of credibility, and the relationship moves to its second phase. At the beginning of this phase, the optimal contract calls for standardization of the work process. The firm implements the rules and asks the worker to take the rigid action. Since the rigid action is less costly to the worker than the adaptive one, it can be induced with relatively weaker incentives. Once the shock passes and the firm pays its promised reward, credibility is restored and discretion is given back to the worker. Hence, as the firm's credibility evolves in response to shocks, the firm oscillates between fostering worker initiative and requiring adherence to rules.

But once the standardized work process is put in place, the nature of the relationship changes: the relationship becomes less efficient and more vulnerable to future shocks. After the introduction of standardized processes, it becomes more difficult to encourage the worker to take initiative in the future. When discretion is given back to the worker, he can now deviate and take the cheaper rigid action (instead of the adaptive one, which is more costly), since he now knows that the rigid action might still yield a high output. Thus, the moral hazard problem aggravates, and in order to induce the adaptive action, the firm must offer rents to the worker. As the worker earns a rent, the firm's value of the relationship decreases. Consequently, the worker's trust in the firm deteriorates, and so does the relationship's ability to endure future shocks. It becomes more likely that an inefficient action (i.e., either the rigid action or termination) will be used if shocks arise in the future, and the joint surplus in the relationship shrinks even after the relationship recovers from the current shock.

Further shocks, if sufficiently severe, move the relationship to its final phase, where the firm's value of the relationship becomes so low that the firm cannot even credibly offer the incentives needed to elicit the rigid action. At this point, the relationship is terminated.

The dynamics of the optimal contract brings to the fore two novel aspects of the use of rules. First, though rules help the relationship in times of stress, the resulting strain inflicts a cost on the relationship's future. Even after the firm regains its credibility and gives back discretion to the worker, the relationship continues to bear the scars of past shocks and never recovers completely: while the relationship may appear to revert back to its initial form (with the worker again taking the adaptive action), it endures a structural change and becomes more fragile to future shocks.

Second, in response to the shocks, the firm may be compelled to use the standardized work process (i.e., the rigid action) when the strong incentives needed to encourage employee initiative are no longer feasible. However, we show that the standardization of the work process may also be called for as a precautionary measure, even when incentives for worker initiative (i.e., the adaptive action) are still feasible. This is due to the fact that shocks are more damaging to the relationship when the worker is urged to take the adaptive action. Since the adaptive action requires stronger incentives, the firm must promise a larger reward, and this promise is only credible if the firm is punished severely if it reneges. Thus, when shocks arise, the firm's stake in the relationship erodes faster, and so does its credibility with the worker. Standardization slows the relationship's decay caused by future shocks because the rigid action requires weaker incentives; for such incentives to be credible, punishments need not be too harsh. As a result, the relationship can survive a longer spell of consecutive shocks before it must face termination.

While we illustrate the long-term implications of rules by using a model of employment relationship, one may consider several other contractual settings where similar dynamics can emerge. Indeed, a key aspect of our argument (i.e., the erosion of the relationship's value may necessitate the adoption of rules) is applicable in a wide range of environments. For example, in relationships between firms such as supply chains and joint ventures, production efficiency may require that the parties have flexibility to respond to local information. Consequently, it may not be optimal to stipulate rules if the parties can be incentivized to put in consummate effort and respond to underlying circumstances appropriately. But if the value of the relationship decreases, incentives for consummate effort may not be feasible, and the parties may optimally stipulate rules that can still elicit a moderate level of effort and also arrest the decay of the relationship. Similarly, a regulatory agency in charge of overseeing a firm's product safety may allow the firm considerable discretion on product design but impose large penalties if the product harms the consumers. But incentives through such large penalties may be feasible only if the regulator-firm relationship is sufficiently valuable as otherwise the firm may be liquidity constrained. Hence, if the value of the relationship

depletes, the regulator may stipulate minimum safety standards that could be enforced with weaker incentives.

In all such settings, adoption of rules can be an effective coping strategy when the relationship's value depletes due to negative shocks. The rules ensure that all parties continue to deliver a minimum level of performance by simply following a standardized work process. But, our findings highlight a long-term cost of such standardized processes—once those involved learn that following these processes is an acceptable compromise, it becomes harder to incentivize them to go beyond the rules in the future.

Related literature: It has been long recognized that decentralized decision-making improves economic efficiency: The economic agents, when free from strict control by rules, can adapt their actions to decision-relevant information that resides locally (Hayek, 1945). But the economics and the management literature point to various reasons why the firms may still resort to rule-based work and succumb to organizational rigidities. Work routines may minimize misunderstanding and facilitate coordination (Nelson and Winter, 1982); adherence to norms can effectively guide behavior and reaffirm reputation in unforeseen circumstances (Kreps, 1990); and rigidities can also emerge from the agents' incentives to exploit existing business opportunities rather than to explore new ones so as to protect their current rents (Holmström, 1989; Henderson, 1993; Schaefer, 1998; also see Garicano and Rayo, 2016, for a survey).

Several scholars have also argued that it is less costly for the employees to follow rules than to use their discretion, and rules can be useful when employees cannot be trusted to use their discretion judiciously (Holmström, 1984; Bowen and Lawler, 1992; Alonso and Matouschek, 2007, 2008). In addition, the law and economics literature makes a related point in the context of enforcing legal commands. Commands promulgated as rules (as opposed to “legal standards”) are easier to follow but incentivize the individuals to merely act as per the stated rules even if they fail to meet the standards (Kaplow, 1992; Sullivan, 1992; Sunstein, 1995; Posner, 2002).

We contribute to this literature by highlighting how the adoption of new rules may inflict a dynamic cost on the organization as the rules play a dual informational role. By providing information on a standardized work process that is invariant to local conditions, rules lower the workers' effort cost and save the organization during time of crisis. But once such rules are in place, the workers also learn what compromises may be tolerated by the organization. As a consequence, in the future, the organization ends up relying on such rules too frequently and becomes more bureaucratic as its attempts to revert back to the earlier adaptive mode fail more easily.

Thus, we offer a novel explanation why organizations become more rigid over time in spite of their efforts to remain flexible. In particular, we show how a firm’s incentive structure may coevolve with its organizational design and make it harder for the firm to adapt its established routines and culture in the face of environmental changes.³

Our paper also contributes to a growing literature on the dynamics of employment relationships. Models of relational contracts have been used to show how relationships may improve over time as parties learn to coordinate more effectively (Watson, 1999, 2002; Chas-sang, 2010; Halac, 2014). Cooperation may also deteriorate due to a worsening production environment (Garrett and Pavan, 2012; Halac and Prat, 2016) or inefficient allocation of authority that emerges as a compromise for past events (Li, Matouschek, and Powell, 2017). Finally, relationships can cycle between phases of reward and punishment when parties may have private information (Li and Matouschek, 2013; Zhu, 2013; and Fong and Li, 2017).

In our model, the relationship also oscillates between using an adaptive action and a rigid one, but the rigid action ushers in a structural change when it is first introduced; once this action is made available, the future surplus in the relationship is irrecoverably compromised. This feature of our model also necessitates a novel methodological approach. Typically, the relational contracting models of employment dynamics relies on the standard recursive method à la Abreu et al. (1990) in order to characterize the equilibrium payoff set. But such a method cannot be directly used in our setting as the introduction of the rigid action expands the agent’s action set, and the timing of its introduction is also endogenous to the model. In particular, the characterization of the equilibrium payoff set prior to the introduction of the rigid action must account for two important issues: first, the equilibrium payoff set depends on the (optimal) timing for the introduction of the rigid action, and second, the recursive structure of the equilibrium payoff set is affected by the fact that the continuation payoffs may reside in a different payoff set—one that is associated with the game when the rigid action is already available.

The trade-offs with rules and initiative that we explore are reminiscent of a few related strands of literature in organizational economics. First, the literature on the relative merits of decentralization and centralization also speaks to the value of rule-based work (as rules are

³There is little work on the interplay between an organization’s design and its culture, but one recent exception is Besley and Persson (2017). In their framework, the organizational culture is reflected by the relative sizes of different groups of managers where members in each group hold a set of common values. They show how the social identities of overlapping generations of managers can evolve with the organization’s decentralization decision, leading to a co-movement of organizational design and its culture.

often formulated as a part of a centralized decision-making process). This literature highlights a trade-off between coordination and adaptation: Centralization facilitates coordination between different divisions of an organization (Chandler, 1977), but impedes adaptation to local information. Relatedly, several authors have studied how the junior managers may be incentivized to accurately report their local information to the top management (Aghion and Tirole, 1997; Alonso, Dessein, and Matouschek, 2008; also see Gibbons, Matouschek, and Roberts, 2012, for a survey).

Second, there is a vast literature on the interaction between formal and informal incentives that presents an interesting contrast to our setup (see, e.g., Baker, Gibbons, and Murphy, 1994; Schmidt and Schnitzer, 1995; Che and Yoo, 2001). This literature assumes that an agent’s private action is reflected in multiple performance signals, some of which are verifiable and some of which are not (a recent exception is Kvaløy and Olsen, 2009, who present analysis of endogenous verifiability). The optimal incentive scheme, therefore, combines court-enforceable incentive contracts with relational incentives sustained through repeated interactions. Moreover, the two forms of incentives could be substitutes or complements depending on the underlying economic environment. In our setting, formal contracts are infeasible irrespective of whether rules are used or not, and the dynamics of worker initiative is driven by the dynamics of the optimal relational contract.

Finally, our analysis may also remind the reader of Bernheim and Whinston’s (1998) argument for “strategic ambiguity”. Bernheim and Whinston show that when only some aspects of an agent’s job are verifiable and some are not, the formal contract may leave even the verifiable aspects of the job unspecified. Such contractual incompleteness allows the employer to adjust the contract terms *ex post* in response to the agent’s performance on the non-verifiable aspects of the job, and it generates stronger incentives for all aspects of the job *ex ante*. In contrast, we consider a setting where the employer may opt to leave the work rules vague so as to encourage the worker to take initiative and ensure production efficiency. In our model, job performance is unidimensional and non-verifiable; hence, incentives are always relational, and we focus on the dynamics of worker initiative in the optimal contract.

2. MODEL

A principal (or “firm”) hires an agent (or “worker”) where the two parties enter in an infinitely repeated employment relationship. Time is assumed to be discrete and denoted as $t \in \{1, 2, \dots, \infty\}$. In each period, the principal and the agent play a stage game that is defined as follows.

Stage game: We elaborate on the stage game by describing its three key components: *Technology*, *contracts*, and *payoffs*.

TECHNOLOGY: The agent must take an (private) action a_t to perform a job. The job requires the agent to execute a set of tasks T that he may potentially choose from a set $\mathbb{T} \subseteq \mathbb{R}$. The job output $Y_t \in \{-z, 0, y\}$ depends on how well the set of executed tasks $T \subset \mathbb{T}$ aligns with the underlying state of the world $\omega_t \in \Omega \subset \mathbb{R}$. The state of the world is not publicly observable, and it is identically and independently distributed across periods. The agent can always choose an “adaptive” action a_A where he takes initiative to *first* (privately) learn the realization of ω_t , and *then* carry out the set of tasks $T_{\omega_t} \subset \mathbb{T} \subseteq \mathbb{R}$ that is most appropriate under the observed state. Executing the “most appropriate” set of tasks (i.e., doing T_{ω_t} when the state is ω_t) guarantees a high output (i.e., $Y_t = y$).

The agent can also choose a “rigid” action a_R where he follows a set of rules that standardize the work process, but only if these rules are put in place by the principal. The standardized procedure requires the agent to perform a prespecified set of tasks T_R regardless of the underlying state of the world, and yields a high output ($Y_t = y$) with probability $p \in (0, 1)$ and low output ($Y_t = 0$) with probability $1 - p$.

For any state ω_t , performing an arbitrarily chosen set of tasks $T \subset \mathbb{T}$ that is neither the appropriate set T_{ω_t} nor the standardized procedure T_R results in a considerable damage to the firm as it yields $Y_t = -z$. We assume that the set of states Ω and the set of all possible tasks \mathbb{T} are both sufficiently large, and the players’ prior belief over Ω is sufficiently diffused so that any set of tasks T that is chosen without the exact knowledge of the underlying state or the standard procedure will be (almost surely) distinct from both T_{ω_t} and T_R . Thus, the adaptive and the rigid actions are the only two productive actions that the agent can undertake.

Both the adaptive and the rigid action are costly to the agent. The agent incurs a cost of action $c(a_t)$ where $c(a_A) = C$ and $c(a_R) = c$. We assume that $C > c > 0$; the adaptive action is costlier as it requires the agent to learn the underlying state in order to direct his efforts accordingly. The agent may also shirk by choosing a costless action a_S , that also damages to the firm’s value and yields $-z$.

The principal, in contrast, can establish the standard procedure (and introduce the rigid action) at zero cost. By introducing the rigid action, the principal effectively imparts knowledge to the agent about a “short-cut” in the production process—one that compromises the production efficiency but can still deliver an acceptable level of output. Therefore, once the agent learns the standard procedure, he may choose to follow it in the future even when he is asked to exert consummate effort.

While the agent's action is his private information, the output Y_t is publicly observable, though non-verifiable. We denote the availability of the standard procedure as $\gamma_t \in \{0, 1\}$, where $\gamma_t = 1$ if a procedure has been put in place and $\gamma_t = 0$ otherwise.

CONTRACT: In each period t , the principal decides on whether to offer a contract to the agent. Let $d_t^P \in \{0, 1\}$ denote the principal's offer decision where $d_t^P = 0$ if no offer is made and $d_t^P = 1$ otherwise. The principal also decides whether to put in place a standard work procedure at the beginning of the period, if it has not been done in the past.

As the job output Y_t is non-verifiable, explicit pay-per-performance contracts are not feasible. Instead, the principal offers a relational contract that specifies a discretionary bonus b_t that depends on Y_t . The agent is liquidity constrained, and b_t must be non-negative. We assume that the principal's ability to pay the agent is stochastic as she may be exposed to a liquidity shock. In absence of any shock the opportunity cost of a dollar is a dollar whereas if there is a shock, the opportunity cost is prohibitively high and the principal cannot make any payments to the agent. Let $\rho_t \in \{S, N\}$ be the realization of the liquidity shock in period t , where $\rho_t = S$ if there is a shock and $\rho_t = N$ if there is none. We assume that ρ_t is identically and independently distributed across periods and $\Pr(\rho_t = S) = \theta \in (0, 1)$. The liquidity shock is privately observed by the principal after the realization of the output. As the principal cannot pay the agent anything if there is a liquidity shock, the agent's compensation does not include any contractual wage component.⁴

Upon receiving the contract offer, the agent decides whether to accept it or not. Let $d_t^A \in \{0, 1\}$ denote the agent's decision where $d_t^A = 0$ if the offer is rejected and $d_t^A = 1$ if it is accepted. Upon accepting the offer, the agent decides on his action a_t .

Finally, we assume that there is a public randomization device, generating a realization $x_t \in [0, 1]$ at the end of the period. We may assume that the public randomization device is also available at the beginning of the game.

The timing of the stage game is summarized below.

- *Beginning of Period t .* The principal decides whether or not to offer a contract to the agent. If a contract is offered, the principal also decides on whether to establish

⁴Our assumptions on the liquidity shock are reminiscent of Li and Matouschek (2013), and such shocks may emanate from the volatility in the credit market or unexpected arrival of new business opportunities that require a large investment. We adopt this modeling specification due to its analytical tractability but the specific nature of the shock is not a critical aspect of the model. A similar trade-off with the introduction of rule and the associated contractual dynamics can potentially emerge due to other types of shocks that create a friction in transfers between the contracting parties.

the standardized work procedure (if such procedure has not been set up yet) and the game moves to period $t.1$. If no contract is offered, the game moves to period $t + 1$.

- *Period t.1.* The agent either accepts or rejects the contract offered by the principal. If he accepts, the game moves to period $t.2$. If he rejects, the game moves to period $t + 1$.
- *Period t.2.* The state of the world ω_t is realized and the agent chooses the action a_t . If a standardized procedure is in place $a_t \in \{a_A, a_R, a_S\}$ and if it is not $a_t \in \{a_A, a_S\}$.⁵
- *Period t.3.* The output Y_t is observed.
- *Period t.4.* The principal privately observes the liquidity shock ρ_t .
- *Period t.5.* The principal decides on the bonus payment. A bonus may be paid if there is no shock.
- *End of Period t.* The outcome of the randomization device x_t is realized and the game moves to period $t + 1$.

PAYOFFS: The principal and agent are risk neutral. If either d_t^P or d_t^A is 0, both receive their outside options in that period—which we assume to be 0 for both—and the game moves on to period $t + 1$. If $d_t^A = d_t^P = 1$, for a given action a_t of the agent, the agent and the principal earn:

$$\hat{u}_t = \mathbb{E} [1_{\{\rho_t=N\}} b_t(Y_t) \mid a_t] - c(a_t)$$

and

$$\hat{\pi}_t = \mathbb{E} [Y_t - 1_{\{\rho_t=N\}} b_t(Y_t) \mid a_t],$$

respectively, where the expectation is taken using the distribution of ρ_t and Y_t conditional on a_t .

Repeated game: The stage game described above is repeated every period and both the agent and the principal have a common discount factor $\delta \in (0, 1)$. At the beginning of any period t , the normalized payoffs of the players in the continuation game are given as:

$$u^t = (1 - \delta) \sum_{\tau=t}^{\infty} \delta^{\tau-t} d_{\tau} \hat{u}_{\tau} \text{ and } \pi^t = (1 - \delta) \sum_{\tau=t}^{\infty} \delta^{\tau-t} d_{\tau} \hat{\pi}_{\tau},$$

where $d_{\tau} := d_{\tau}^A d_{\tau}^P$.

⁵The stated action sets are without any loss of generality as the agent would always prefer shirking (i.e., choose a_S) to performing an arbitrary set of tasks $T \notin \{T_{\omega_t}, T_R\}$ (both actions yield the same output $-z$, but the latter would entail a strictly positive cost).

STRATEGIES AND EQUILIBRIUM: As standard in the literature (see, e.g., Levin, 2003) we define a relational contract as a pure strategy public Perfect Equilibrium (PPE) where the players only use public strategies, and the equilibrium strategies induce a Nash Equilibrium in the continuation game starting from each public history. A public strategy of the principal stipulates her participation decision, decision on whether to put in place the standardized work procedure, and decision on the bonus payment in each period as a function of the public history of the game. Similarly, a public strategy for the agent stipulates his participation and action decisions in each period given the public history. We define an optimal relational contract as a PPE of this game where the payoffs are not Pareto-dominated by any other PPE.

In what follows, we maintain a few restrictions on the parameters in order to focus on a more interesting modeling environment.

Assumption 1. (i) $y - C > py - c > 0$; (ii) $pC > c$; (iii) $(1 - \delta)(1 - p) > \delta p\theta$ and $y > \max \left\{ \frac{1}{\delta(1-\theta)}, \frac{1-\delta}{(1-\delta)(1-p)-\delta p\theta} \right\} K$, where $K := ((C - c) - \delta(1 - \theta)(pC - c)) / (1 - p)$; (iv) $z > \frac{\delta}{1-\delta}(y - C)$.

Assumption 1 (i) ensures that the adaptive action (a_A) is more efficient than the rigid one (a_R), which is, in turn, more efficient than dissolving the employment relationship. Parts (ii) and (iii) ensure that both the adaptive and the rigid actions are used on the equilibrium path, and the optimal relational contract gives rise to a rich set of dynamics. Part (ii) requires the adaptive action to be sufficiently more costly than the rigid action, whereas part (iii) stipulates that neither δ nor p is too large, and when the job is successfully completed, the value of the output is sufficiently high (the term on the right gives a sufficient lower bound). Finally, part (iv) ensures that it is never optimal to ask the agent to shirk on the equilibrium path as the damage from shirking is sufficiently large.

Since the introduction of the standardized procedure is a part of the principal's strategy, the analysis of the optimal relational contract requires a complete characterization of the equilibrium payoff set both before and after the principal introduces this procedure. The characterization results in these two scenarios are presented in the next two sections.

3. EQUILIBRIUM PAYOFF SET AFTER ESTABLISHING THE STANDARDIZED PROCEDURE

Suppose that the principal has already put in place the rules that standardize the work process; i.e., the agent knows the set of tasks (T_R) that constitute the rigid action. Let \mathcal{E}_r be the PPE payoff set (for a given δ). We characterize \mathcal{E}_r using the recursive method à la Abreu et al. (1990). Any equilibrium payoff pair $(\pi, u) \in \mathcal{E}_r$ is supported either by a pure

action profile in the stage game together with a set of continuation payoffs that the players expect to receive in the future, or by randomizing over a set of equilibrium payoff pairs that are themselves supported by some pure action profiles (in the stage game).

In a pure action profile in the stage game, the players can take the outside option, in which case both parties receive 0. The parties can also enter the relationship, in which case, the agent will take either the adaptive action or the rigid action (by Assumption 1 (iv), it is never optimal for the principal to hire the agent and ask him to shirk). We denote these two action profiles, with a slight abuse of notation, as A and R , respectively. Also, we denote $a = O$ when the parties take the outside option. For any current period action $a \in \{A, R\}$, let b^a be the associated bonus to the agent when there is no liquidity shock. Also, let $(\pi_s^a, \pi_n^a, u_s^a, u_n^a)$ be the associated continuation payoffs where π_s^a and π_n^a are the principal's continuation payoff in the shock and no-shock states, respectively, and u_s^a and u_n^a are the same for the agent. Finally, let (π^O, u^O) be the continuation payoffs of the two parties when $a = O$.

Below, we first present the set of constraints that the bonus and the continuation payoffs must satisfy if an action $a \in \{A, R, O\}$ is used to support an equilibrium payoff pair $(\pi, u) \in \mathcal{E}_r$. Next, using these constraints, we characterize the frontier of \mathcal{E}_r .

3.1. The constraints. For any equilibrium payoff pair (π, u) that is supported by an action profile $a \in \{A, R, O\}$ in the current period, the associated stage game play and the continuation payoffs must be such that: (i) the proposed course of the play indeed offers the said payoff (π, u) to the players, and (ii) neither party has any incentive to deviate from the proposed play in the stage game. These requirements give rise to a set of constraints for each one of the three pure action profiles in the stage game, A , R , and O .

ADAPTIVE ACTION. A payoff pair (π, u) can be supported by playing the adaptive action in the current period ($a_t = a_A$) if the following constraints are satisfied.

Promise-keeping: The consistency of the PPE payoff decomposition requires that the players' payoffs must be a weighted average of their current period payoff and the continuation payoff. Without loss of generality, we assume that when the principal wants to implement the adaptive action, the bonus b^A is paid if and only if $Y = y$. Hence, we must have:

$$(PK_A^A) \quad u = \theta [(1 - \delta)(-C) + \delta u_s^A] + (1 - \theta) [(1 - \delta)(b^A - C) + \delta u_n^A]$$

for the agent, and

$$(PK_P^A) \quad \pi = \theta [(1 - \delta) y + \delta \pi_s^A] + (1 - \theta) [(1 - \delta) (y - b^A) + \delta \pi_n^A]$$

for the principal.

No deviation: In equilibrium, neither party should have incentives to deviate from the proposed play, irrespective of whether such a deviation is publicly observed (“off-schedule”) or not (“on-schedule”). Following an off-schedule deviation, without loss of generality, we may assume that the players take their outside options as it constitutes the harshest punishment for both players. Notice that the principal may deviate off-schedule by reneging on its bonus promise even after he reports a “no-shock” state. Consequently, we have the following non-reneging constraint on the principal:

$$(NR^A) \quad -(1 - \delta) b^A + \delta \pi_n^A \geq 0.$$

The principal may also deviate off-schedule by not offering a contract to the agent. The agent, on the other hand, deviates off-schedule if he rejects the principal’s offer. Hence, the individual rationality constraints:

$$(IR) \quad \pi \geq 0, \quad u \geq 0.$$

But both the principal and the agent may also deviate on-schedule. The principal may be tempted to report a liquidity shock when there is none so as to save on the bonus pay. As a result, we have the following “truth telling” constraint:

$$(TT^A) \quad -(1 - \delta) b^A + \delta \pi_n^A \geq \delta \pi_s^A.$$

The agent, on the other hand, may deviate and choose to take the rigid action ($a_t = a_R$) instead of the more costly adaptive action ($a_t = a_A$). Therefore, the following incentive compatibility constraint must hold:

$$u \geq p [\theta ((1 - \delta) (-c) + \delta u_s^A) + (1 - \theta) ((1 - \delta) (b^A - c) + \delta u_n^A)] + (1 - p) (1 - \delta) (-c).$$

Using (PK_A^A) , we can simplify this constraint as:

$$(IC^A) \quad u \geq \frac{1-\delta}{1-p} (pC - c) =: u^*.$$

Notice that as $pC - c > 0$ (by Assumption 1 (ii)), (IC^A) implies that the agent must be given rents if the principal were to induce him to take the adaptive action when the rigid action is available to him. As $u \geq 0$, a deviation to completely shirking on the job ($a_t = a_S$) is never profitable for the agent.

Feasibility: For the equilibrium payoff to be feasible, the associated bonus payment must be non-negative:

$$(NN^A) \quad b^A \geq 0,$$

and the continuation payoffs themselves must be feasible, i.e., the following self-enforcing constraint must hold:

$$(SE^A) \quad (\pi_\rho^A, u_\rho^A) \in \mathcal{E}_r, \rho \in \{S, N\}.$$

RIGID ACTION. Now suppose that a payoff pair (π, u) is supported by playing the rigid action in the current period. As in the case of adaptive action, a similar set of constraints must hold.

Promise-keeping: Without loss of generality, we assume that the bonus b^R is paid if and only if $Y \in \{0, y\}$. Hence, the promise-keeping constraints take the following form:

$$(PK_A^R) \quad u = \theta [(1-\delta)(-c) + \delta u_s^R] + (1-\theta) [(1-\delta)(b^R - c) + \delta u_n^R],$$

and

$$(PK_P^R) \quad \pi = \theta [(1-\delta)py + \delta \pi_s^R] + (1-\theta) [(1-\delta)(py - b^R) + \delta \pi_n^R].$$

No deviation: As discussed earlier, the non-reneging constraint on the principal and the individual rationality constraint on both players must hold in order to deter off-schedule deviations. That is, we require:

$$(NR^R) \quad -(1 - \delta)b^R + \delta\pi_n^R \geq 0,$$

and

$$(IR) \quad \pi \geq 0, \quad u \geq 0.$$

Similarly, the truth-telling constraint on the principal ensures no on-schedule deviation by misreporting the state:

$$(TT^R) \quad -(1 - \delta)b^R + \delta\pi_n^R \geq \delta\pi_s^R.$$

Notice that the agent's incentive compatibility constraint is trivially satisfied as deviating and taking the adaptive action would yield the same expected benefit (as that of taking the rigid action) but at a higher cost. Again, as $u \geq 0$, deviating to a_S (i.e., shirking) is never profitable.

Feasibility: As before, we have the non-negativity constraint and the self-enforcing constraint:

$$(NN^R) \quad b^R \geq 0,$$

and

$$(SE^R) \quad (\pi_\rho^R, u_\rho^R) \in \mathcal{E}_r, \quad \rho \in \{S, N\}.$$

OUTSIDE OPTION. Finally, if a payoff pair (π, u) is supported by players taking their respective outside options in the current period, the following set of constraints must hold.

Promise-keeping: We have:

$$(PK^O) \quad u = \delta u^O \text{ and } \pi = \delta \pi^O.$$

Feasibility: The following self-enforcing constraint hold:

$$(SE^O) \quad (\pi^O, u^O) \in \mathcal{E}_r.$$

3.2. Properties of the PPE payoff frontier. Define the PPE payoff frontier $U_r(\pi)$ as:

$$U_r(\pi) := \sup \{u \mid (\pi, u) \in \mathcal{E}_r\}.$$

The following lemma presents a set of general characteristics of the PPE payoff set.

Lemma 1. *The PPE payoff set \mathcal{E}_r has the following properties: (i) it is compact, (ii) $U_r(\pi)$ is concave, and (iii) for any payoff pair $(\pi, U_r(\pi))$, the associated continuation payoffs (along the equilibrium path) remain on the frontier; i.e., for $a \in \{A, R\}$, $u_s^a = U_r(\pi_s^a)$; $u_n^a = U_r(\pi_n^a)$; and $u^O = U_r(\pi^O)$.*

For Part (i), the compactness of \mathcal{E}_r follows from the fact that there are only a finite number of actions that the agent may be asked to undertake in any equilibrium (i.e., $a \in \{A, R, O\}$), and the transfer from the principal to the agent is essentially bounded by the total future surplus of the relationship. For Part (ii), the presence of the public randomization device ensures concavity of $U_r(\pi)$. The final part of the above lemma shows that, under an optimal relational contract, the continuation payoffs never fall below the frontier. Since both the principal's actions and the agent's performance are publicly observed, there is no need for joint punishment along the equilibrium path.

For our analysis, it is also useful to define the agent's highest payoff for a given payoff of the principal in the set of all PPE that are supported by a specific action. For any $a \in \{A, R, O\}$, let

$$u_r^a(\pi) := \max \{u \mid (\pi, u) \in \mathcal{E}_r \text{ and is supported by } a\}.$$

In particular, for $a \in \{A, R\}$, $u_r^a(\pi)$ satisfies the following:

$$u_r^a(\pi) = \max_{b^a, \pi_s^a, \pi_n^a} (1 - \delta) [(1 - \theta) b^a - c(a)] + \delta [(1 - \theta) U_r(\pi_n^a) + \theta U_r(\pi_s^a)]$$

$$\text{subject to } (PK_P^a), (NR^a), (TT^a), (NN^a), \text{ and } (SE^a).$$

(Clearly, $u_r^a(\pi)$ is defined only for the values of π such that the corresponding (IC^a) constraint is satisfied.) Also notice that:

$$u_r^O(\pi) = \delta U_r(\pi^O), \text{ where } \pi^O = \pi/\delta.$$

Furthermore, notice that the PPE payoff frontier U_r is the function that satisfies the following: Let $\bar{\pi}_r := \max \{ \pi \mid (\pi, u) \in \mathcal{E}_r \}$, i.e., $\bar{\pi}_r$ is the highest PPE payoff to the principal when the standardized work process has already been established. Then, for all $\pi \in [0, \bar{\pi}_r]$,

$$U_r(\pi) = \max_{\alpha_a \geq 0, \pi_a \in [0, \bar{\pi}_r]} \sum_{a \in \{A, R, O\}} \alpha_a u_r^a(\pi_a)$$

s.t. $\sum_{a \in \{A, R, O\}} \alpha_a = 1$, and $\sum_{a \in \{A, R, O\}} \alpha_a \pi_a = \pi$.

In order to characterize the frontier U_r , we first describe, for each action taken, the associated continuation payoffs for the principal.

Lemma 2. *Consider an equilibrium payoff pair (π, u) that is on the payoff frontier $U_r(\pi)$. The following holds:*

(i) *If (π, u) is supported by the adaptive action, then*

$$\pi_s^A(\pi) = \frac{1}{\delta} (\pi - (1 - \delta)y) < \pi \text{ and } \pi_n^A(\pi) = \bar{\pi}_r \geq \pi,$$

and if there is no shock, the principal pays a bonus $b^A(\pi) = y - (\pi - \delta\bar{\pi}_r) / (1 - \delta)$.

(ii) *If (π, u) is supported by the rigid action, then*

$$\pi_s^R(\pi) = \frac{1}{\delta} (\pi - (1 - \delta)py) < \pi \text{ and } \pi_n^R(\pi) = \bar{\pi}_r \geq \pi,$$

and if there is no shock, the principal pays a bonus $b^R(\pi) = py - (\pi - \delta\bar{\pi}_r) / (1 - \delta) > 0$.

(iii) *If (π, u) is supported by the outside option, then*

$$\pi^O(\pi) = \pi / \delta.$$

Part (i) and (ii) of the above lemma state that the principal's continuation payoff decreases in a shock state and increases in a no-shock state. Such a spread between the continuation payoffs in the two states induces the principal to report the state truthfully. However, as we will argue below, when the principal's continuation payoff is sufficiently low, following a shock, an inefficient action—either through the rigid action or the outside option—must be taken. To minimize the likelihood of that such inefficiency would arise, the principal's continuation payoff in a no-shock state jumps to the maximal PPE payoff ($\bar{\pi}_r$) which gives

her the most cushion for future shocks.⁶ Finally, notice that part (iii) directly follows from the principal's promise-keeping constraint when the outside option is used.

Proposition 1 below characterizes the payoff frontier U_r .

Proposition 1. *The payoff frontier U_r can be divided into four regions. There exist cutoffs $0 < \pi_r^O \leq \pi_r^R \leq \pi_r^A \leq \bar{\pi}_r$, with $\pi_r^O < \bar{\pi}_r$, such that:*

(i) *For $\pi \in [0, \pi_r^O)$, the payoff frontier is linear and supported by randomization between $(0, 0)$ and $(\pi_r^O, U_r(\pi_r^O))$. We have $U_r(0) = 0$ and the payoff $(0, 0)$ is supported by $a = O$ (i.e., players taking the outside option).*

(ii) *For $\pi \in [\pi_r^O, \pi_r^R]$, $U_r(\pi) = u_r^R(\pi)$ (i.e., the payoff frontier is supported by the rigid action).*

(iii) *For $\pi \in (\pi_r^R, \pi_r^A)$, the payoff frontier is linear and supported by randomization between $(\pi_r^R, U_r(\pi_r^R))$ and $(\pi_r^A, U_r(\pi_r^A))$.*

(iv) *For $\pi \in [\pi_r^A, \bar{\pi}_r]$, $U_r(\pi) = u_r^A(\pi)$ (i.e., the payoff frontier is supported by the adaptive action), and $U_r(\bar{\pi}_r) = u^*$.*

Figure 1 illustrates the four regions described in Proposition 1. In two regions, one in the middle and one at the right-most end, the payoffs at the frontier are supported by pure actions, by playing $a = R$ and $a = A$, respectively. Also, the $(0, 0)$ payoff pair is the only point on the frontier that is supported by playing $a = O$. In the other two regions, the payoffs are sustained through randomization. Without loss of generality, we assume that in the regions where randomization is used, the players randomize only between the endpoints of the two adjacent regions that are sustained by pure actions.

⁶This pattern of movement in the continuation payoff also occurs in Li and Matouschek (2013) and follows from the same reasoning.

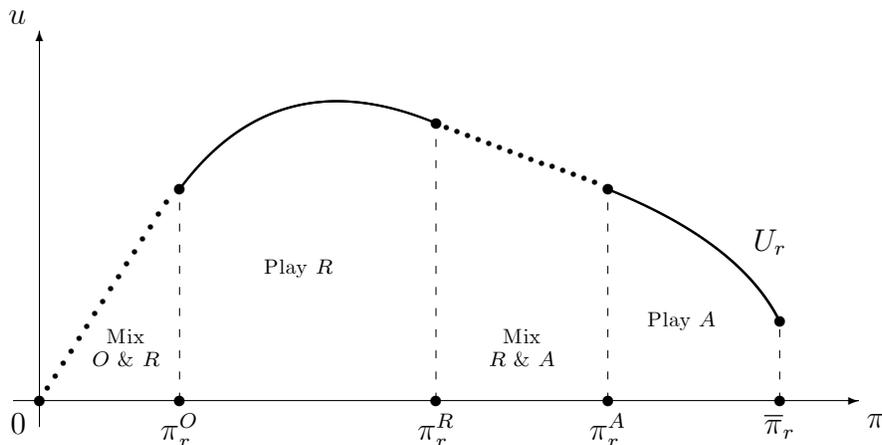


Figure 1. PPE payoff set and frontier when the standardized procedure has already been established.

One feature of the payoff frontier is that the more efficient action gets taken as the principal’s payoff increases. When the principal’s payoff (π) is sufficiently low, i.e., to the left of π_r^O , she does not have enough credibility to promise a bonus large enough to induce the adaptive or the rigid action. When π is above π_r^O , both the rigid and the adaptive action may be feasible. Note that while the adaptive action is more efficient, it gives the principal a lower continuation payoff in shock states (by Lemma 2, $\pi_s^A(\pi) < \pi_s^R(\pi)$), increasing the chance of termination of the relationship. When the principal’s payoff is close to π_r^O , the threat of termination is more imminent, causing the parties to choose the rigid action. In contrast, for a large enough payoff for the principal, the termination is less of a concern, and the adaptive action is chosen.

A notable feature of the PPE frontier U_r is that, at the maximal payoff for the principal ($\bar{\pi}_r$), the agent’s payoff is strictly positive. The reason is that when a standardized work process is established, the moral hazard problem becomes more severe as the agent may deviate and take the rigid action when asked to undertake the more costly adaptive action. To prevent the agent from doing so, the principal must offer him rents. In other words, rules stymie initiative—it gets harder to induce worker initiative once the work rules are standardized.

4. EQUILIBRIUM PAYOFF SET BEFORE ESTABLISHING THE STANDARDIZED PROCEDURE

We now proceed to characterize the set of PPE payoffs, \mathcal{E} , available at the beginning of the game when the principal is yet to put in place the rules, and hence, the standardized

work procedure has not yet been established. A key decision that the principal needs to make is whether or not to introduce these rules upfront. Notice that $\mathcal{E}_r \subseteq \mathcal{E}$. For any payoff $(\pi, u) \in \mathcal{E}_r$, there always exists a PPE where the principal establishes the standardized procedure at the beginning of the game and in the continuation game the parties play the same strategies that give rise to the payoff (π, u) . Furthermore, once the principal decides to establish the standard procedure, the analysis becomes identical to that discussed in the previous section.

But when the principal is yet to introduce the standardized procedure, there are only two actions that the agent can take on the equilibrium path: either take the adaptive action or take the outside option. In this case, any payoff pair $(\pi, u) \in \mathcal{E}$ is supported either by one of these two pure action profiles or by a randomization over the two. We denote these two pure action profiles as $a = \mathcal{A}$, and \mathcal{O} , respectively. (We use different notations than before— $a = \mathcal{A}$ and \mathcal{O} , instead of A and O —in order to distinguish between the use of an action profile when the rigid action is available and when it is not.) In what follows, we only focus on this novel part of the analysis.

4.1. The constraints. As in the previous section, we begin our analysis by presenting the set of constraints that the bonus and the continuation payoffs must satisfy if an action profile $a \in \{\mathcal{A}, \mathcal{O}\}$ is used to support an equilibrium payoff pair $(\pi, u) \in \mathcal{E}$.

ADAPTIVE ACTION: Suppose $(\pi, u) \in \mathcal{E}$ is supported by the adaptive action ($a = \mathcal{A}$). As discussed in Section 3.1, the following promise-keeping constraints must hold:

$$(PK_A^{A*}) \quad u = \theta [(1 - \delta)(-C) + \delta u_s^{\mathcal{A}}] + (1 - \theta) [(1 - \delta)(b^{\mathcal{A}} - C) + \delta u_n^{\mathcal{A}}],$$

and

$$(PK_P^{A*}) \quad \pi = \theta [(1 - \delta)y + \delta \pi_s^{\mathcal{A}}] + (1 - \theta) [(1 - \delta)(y - b^{\mathcal{A}}) + \delta \pi_n^{\mathcal{A}}].$$

The associated no-deviation constraints include the non-reneging and individual rationality constraints for the off-schedule deviations:

$$(NR^{A*}) \quad -(1 - \delta)b^{\mathcal{A}} + \delta \pi_n^{\mathcal{A}} \geq 0,$$

and

$$(IR) \quad u \geq 0;$$

as well as the truth-telling constraint for the on-schedule deviation:

$$(TT^{A*}) \quad -(1 - \delta) b^A + \delta \pi_n^A \geq \delta \pi_s^A.$$

Finally, we have the two feasibility constraints (non-negativity and self-enforcing):

$$(NN^{A*}) \quad b^A \geq 0,$$

and

$$(SE^{A*}) \quad (\pi_\rho^A, u_\rho^A) \in \mathcal{E}, \rho \in \{S, N\}.$$

Note that, unlike the analysis in the previous section, the rigid action is not known to the agent. As a result, if the agent deviates he must choose $a_t = a_S$ and his shirking gets detected for sure. Therefore, the incentive compatibility constraint for the agent's action choice is always satisfied, and hence, we omit it here. Also, the (SE^A) differs from its counterpart in Section 3.1 by requiring the continuation payoffs to be in the payoff set \mathcal{E} instead of \mathcal{E}_r , i.e., the PPE payoff set when the rigid action is available.

OUTSIDE OPTION: If $(\pi, u) \in \mathcal{E}$ is supported by the parties taking the outside option in the current period ($a = \mathcal{O}$), the associated continuation payoffs $(\pi^\mathcal{O}, u^\mathcal{O})$ satisfy the following promise-keeping and self-enforcing constraints:

$$(PK^{\mathcal{O}*}) \quad u = \delta u^\mathcal{O} \text{ and } \pi = \delta \pi^\mathcal{O},$$

and

$$(SE^{\mathcal{O}*}) \quad (\pi^\mathcal{O}, u^\mathcal{O}) \in \mathcal{E}.$$

4.2. Properties of the PPE payoff frontier. As in the previous section, let $U(\pi)$ be the PPE payoff frontier at the beginning of the game (i.e., before the standardized work process is introduced), i.e.,

$$U(\pi) := \sup \{u \mid (\pi, u) \in \mathcal{E}\}.$$

and let $\bar{\pi} := \max \{\pi \mid (\pi, u) \in \mathcal{E}\}$. Also, for any $a \in \{\mathcal{A}, \mathcal{O}\}$, let

$$u^a(\pi) := \sup \{u \mid (\pi, u) \in \mathcal{E} \text{ and is supported by } a\}.$$

The following two lemmas present a set of general properties of the payoff frontier U that mirror those of U_r discussed above.

Lemma 3. *The PPE payoff set \mathcal{E} has the following properties: (i) it is compact, (ii) $U(\pi)$ is concave, and (iii) for any payoff pair $(\pi, U(\pi))$ sustained by pure action $a \in \{\mathcal{A}, \mathcal{O}\}$, the associated continuation payoffs (along the equilibrium path) remain on the frontier; i.e., $u_s^{\mathcal{A}} = U(\pi_s^{\mathcal{A}})$, $u_n^{\mathcal{A}} = U(\pi_n^{\mathcal{A}})$ and $u^{\mathcal{O}} = U(\pi^{\mathcal{O}})$.*

Lemma 4. *Consider an equilibrium payoff pair (π, u) that is on the payoff frontier $U(\pi)$. The following holds:*

(i) *If (π, u) is supported by the adaptive action, then*

$$\pi_s^{\mathcal{A}}(\pi) = \frac{1}{\delta} (\pi - (1 - \delta)y) < \pi \text{ and } \pi_n^{\mathcal{A}}(\pi) = \bar{\pi} \geq \pi.$$

If there is no shock, the principal pays a bonus $b^{\mathcal{A}}(\pi) = y - (\pi - \delta\bar{\pi}) / (1 - \delta) > 0$.

(ii) *If (π, u) is supported by the outside option, then*

$$\pi^{\mathcal{O}}(\pi) = \pi / \delta.$$

The arguments behind the above lemmas closely parallel their counterpart in Lemma 1 and 2 (hence, we omit the formal proofs). Using these lemmas, we derive the following proposition that characterizes the PPE payoff frontier.

Proposition 2. *The payoff frontier U can be divided into four regions. There exist cutoffs $0 < \pi^O \leq \pi^R \leq \pi^A \leq \bar{\pi}$, with $\pi^O < \bar{\pi}$, such that (the notations $u_r^R(\pi)$ and $U_r(\pi)$ are as defined in Proposition 1):*

(i) *For $\pi \in [0, \pi^O)$, the payoff frontier is linear and supported by randomization between $(0, 0)$ and $(\pi^O, U(\pi^O))$. We have $U(0) = 0$ and the payoff pair $(0, 0)$ is supported by $a = \mathcal{O}$ (i.e., with players taking the outside option).*

(ii) *For $\pi \in [\pi^O, \pi^R]$, $U(\pi) = U_r(\pi) = u_r^R(\pi)$ (i.e., the payoff frontier is supported by the rigid action).*

(iii) *For $\pi \in (\pi^R, \pi^A)$, the payoff frontier is linear and supported by randomization between $(\pi^R, U(\pi^R))$ and $(\pi^A, U(\pi^A))$.*

(iv) *For $\pi \in [\pi^A, \bar{\pi}]$, $U(\pi) = u^A(\pi)$ (i.e., the payoff frontier is supported by the adaptive action \mathcal{A}), and $U(\bar{\pi}) = 0$.*

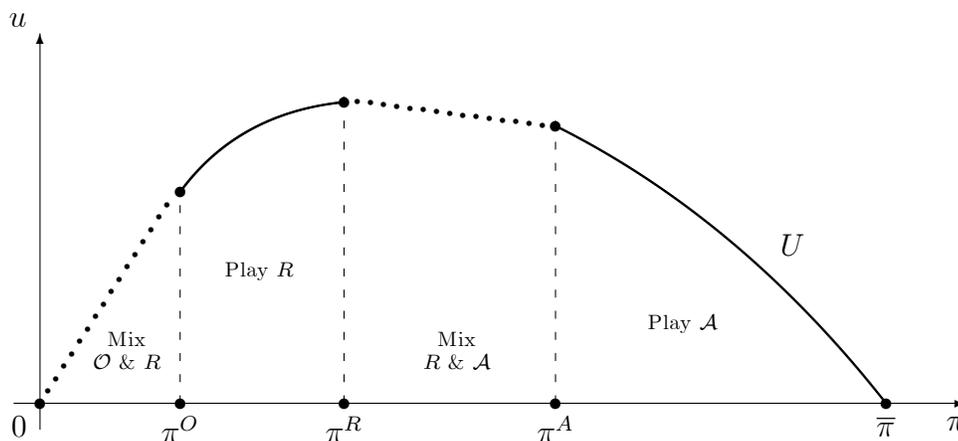


Figure 2. PPE payoff set and frontier before the standardized procedure is established.

This proposition indicates that similar to U_r (the frontier when the standardized process has already been introduced), the frontier U can also be divided into four regions. A pure action is used to sustain payoffs in two of the four regions: a part in the middle is supported by the rigid action where the principal introduces the standardized work process, and the very right-most part of frontier is sustained through the adaptive action where the principal

refrains from introducing the standardized procedure. In addition, the outside option is used only to support the payoff $(0, 0)$. The remaining two regions are supported through randomization. As before, we assume that in such regions the players randomize only between the endpoints of the two adjacent regions that are sustained by pure actions.

The shape of the frontier U is also similar to its counterpart U_r where a more efficient action gets taken as the principal's payoff increases. However, there are some important differences. First, the frontier U indicates not only the agent's action but also the principal's decision on the implementation of the standardized procedure. In particular, whenever the principal's payoff falls below the cutoff π^R , the procedure is put in place with certainty. Second, at the principal's maximal payoff, $\bar{\pi}$, the agent does not earn any rents. This difference arises because at $\bar{\pi}$ the principal has not put in place the standardized procedure, and hence, the agent cannot take a rigid action. Consequently, the underlying moral hazard problem is less severe and the principal need not offer him rents in order to induce him to take the adaptive action. Finally, the cutoffs that define the four regions are, in general, different. This difference in the cutoffs is important as it affects the dynamics of the relationship, which we discuss in the next section.

5. THE DYNAMICS OF THE RELATIONSHIP

Using the results obtained in the previous two sections, we can now discuss the dynamics of the relationship as it may evolve over time in response to the liquidity shocks faced by the principal. We begin by presenting a lemma that helps us contrast the PPE payoff frontiers U_r and U —the ones when the principal has established the standardized procedure and when she has not.

Lemma 5. *We have the following: $\pi^O = \pi_r^O$, $\pi^R \leq \pi_r^R$, and $\bar{\pi} > \bar{\pi}_r$. In addition, $U(\pi) = U_r(\pi)$ for all $\pi \leq \pi^R$ and $U(\pi) > U_r(\pi)$ otherwise.*

This lemma highlights the efficiency loss that results from the establishment of the standardized procedure. The maximal joint surplus that could be obtained in any PPE where $\pi > \pi^R$ is strictly smaller if the standardized procedure is established from the beginning of the game. The loss of surplus stems from the fact that having the standardized procedure in place increases the likelihood that an inefficient action would be taken in the future (in response to shocks) even if the efficient adaptive action is chosen at present.

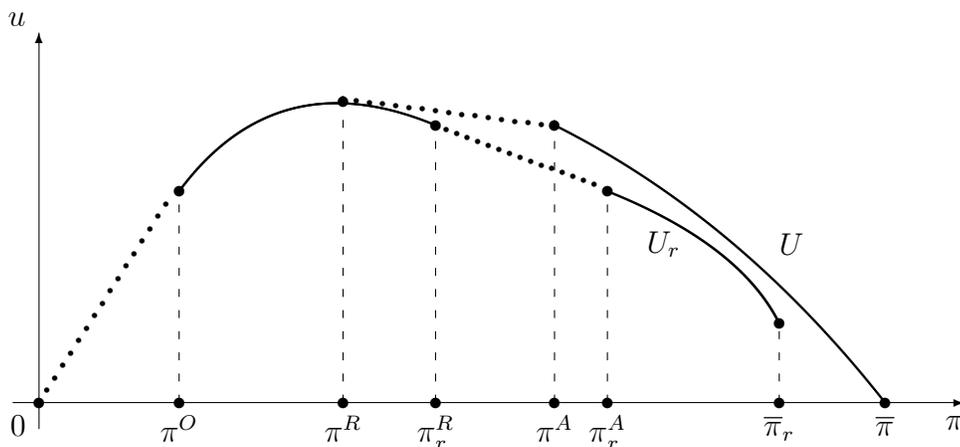


Figure 3. The PPE frontiers U_r and U .

Notice that the thresholds π^O and π^R indicate how far the principal’s continuation payoff needs to fall before each of the two inefficient actions—the outside option and the rigid action, respectively—gets taken if the standardized procedure has not been established already (also, π_r^O and π_r^R represent the corresponding cutoffs when the procedure has been established). Though the threshold for taking the outside option is the same under the two cases, the threshold for taking the rigid action is (weakly) lower.

More importantly, the principal’s maximal PPE payoff is strictly larger if the procedure is not in place than if it is (i.e., $\bar{\pi} > \bar{\pi}_r$). That is, the principal not only can extract more rents from the agent but also the joint surplus is larger if the standardized procedure is not in place to begin with. The arguments for these two observations are closely interlinked. Recall that having the standardized procedure available makes the moral hazard problem more severe. In order to induce the agent to take the adaptive action, the principal must offer him rents (by Proposition 1). As the principal has a smaller continuation value to begin with, it lowers her credibility in promising a large bonus payment that is needed to induce the adaptive action. Consequently, the relationship becomes more vulnerable to shocks and the use of inefficient action becomes more likely in the future, lowering the total surplus in the relationship.

In contrast, if the procedure has not been established yet, the agent does not get any rents when the principal’s payoff is $\bar{\pi}$. The principal is able to better extract rents, giving her

more credibility in promising a bonus. Consequently, the relationship is more resilient to shocks and yields a strictly higher surplus.

Proposition 3. *(The structure and the dynamics of the relationship) The optimal relational contract contains the following three phases.*

(i) *The relationship starts in Phase 1 where: (a) The standardized procedure is never established and the agent always chooses the adaptive action. (b) The principal's payoff π starts at $\bar{\pi}$. (c) For any π , when there is a shock, the principal's payoff decreases to $\pi_s^A(\pi)$. But if there is no shock, the principal pays a bonus $b^A(\pi)$ and his payoff moves to $\bar{\pi}$ (or remains at $\bar{\pi}$ if $\pi = \bar{\pi}$). The relationship stays in this phase as long as $\pi \geq \pi^A$. If $\pi < \pi^A$, the relationship transitions to Phase 2 with positive probability.*

(ii) *In Phase 2: (a) The standardized procedure is established and the agent starts the phase by choosing the rigid action. (b) Whenever the agent chooses the rigid action, if there is a shock, the principal's payoff decreases to $\pi_s^R(\pi)$. But if there is no shock, the principal pays a bonus $b^R(\pi)$ and his continuation payoff moves to $\bar{\pi}_r$ (where the agent chooses the adaptive action). (c) Whenever the agent chooses the adaptive action, if there is a shock the principal's payoff decreases to $\pi_s^A(\pi)$. And if there is no shock, the principal pays a bonus $b^A(\pi)$ and his payoff moves to $\bar{\pi}_r$ (or remains at $\bar{\pi}_r$ if $\pi = \bar{\pi}_r$). (d) The agent chooses the rigid action if $\pi \leq \pi_r^R$, and chooses the adaptive action with a positive probability if and only if $\pi > \pi_r^R$. The relationship stays in this phase as long as $\pi \geq \pi^O$. If $\pi < \pi^O$, the relationship transitions to Phase 3 with positive probability.*

(iii) *In Phase 3, the relationship is terminated.*

The above result follows directly from the characterization of the PPE frontiers discussed in Propositions 1 and 2 (hence, we omit the formal proof). The relationship starts at the right-most point of U : the principal does not establish the standardized procedure, encourage worker initiative by inducing the agent to choose the adaptive action, and extracts all surplus (i.e., $\pi = \bar{\pi}$). If a shock occurs, the continuation payoffs move to the left along the PPE payoff frontier—in order to ensure truthful reporting, the principal must transfer rents to the agent following the announcement of a shock state. Though a no-shock state instantaneously moves the relationship to its initial starting point, as an arbitrarily long stretch of consecutive shocks occurs almost surely, the parties are eventually forced to take an inefficient action.

Once the principal’s payoff falls below π^A , there is a positive probability that she would establish the standardized procedure, and ask the agent to follow it (i.e., take the rigid action). In particular, for lower values of π , the principal may not have sufficient credibility to promise the bonus needed to induce the costly adaptive action, and the rigid action is used with certainty. But once the standardized work process is introduced, the relationship never fully recovers. Even after the shock has passed, the relationship moves to the right-most point of U_r instead of U , where the joint surplus is smaller than what it was at the beginning of the relationship. As before, following more shocks, the continuation payoffs move further to the left. Eventually, the principal loses so much credibility that she cannot even promise the bonus needed to induce the agent to take the rigid action, and the parties may terminate the relationship.

It is also worth noting that the size of the bonus goes down when a less efficient (i.e., less costly) action is taken. Moreover, for a given payoff of the principal, the bonus offered to inducing the adaptive action is larger when the principal is yet to establish the standardized procedure (i.e., $b^A(\pi) > b^A(\pi) > b^R(\pi)$, by Lemma 4 and 2). Because the principal’s maximal PPE payoff is larger when the standardized procedure is yet to be set (i.e., $\bar{\pi} > \bar{\pi}_r$), she can credibly transfer more rents to the agent in a no-shock state.

Two important implications of the above findings—as given in the proposition below—further illustrate the trade-offs with establishing the standardized procedure.

Proposition 4. *The optimal relational contract has the following features:*

(i) *The rigid action may be used when the adaptive action is still feasible. Moreover, the set of parameters for which this is the case is larger when the standardized procedure has already been established in the past than when it has not.*

(ii) *The number of consecutive shocks that guarantees that the rigid action is used when the relationship starts in Phase 1 (with $\pi = \bar{\pi}$ as the standard process is yet to be established) is at least as large as its counterpart when the relationship restarts after reaching Phase 2 (with $\pi = \bar{\pi}_r$ where the standard process has already been established).*

We have argued above that in response to a current shock the rigid action may be used as the principal may not have enough reputational capital to incentivize the agent to undertake the more costly adaptive action. But the first part of Proposition 4 states that in response to shocks the relationship may switch to rigid action as a “precautionary measure”—even if the principal could still induce the agent to take the adaptive action, the rigid action is called

for. The intuition can be traced from the continuation payoffs in a shock state as given in Lemma 4 and 2. For a given payoff of the principal the associated continuation payoff in a shock state is smaller when the adaptive action is being used compared to the case when a rigid action is being used (i.e., $\pi_s^A(\pi) < \pi_s^R(\pi)$). So, by using the rigid action instead of the adaptive one the contracting parties can arrest the erosion of surplus in the relationship as shocks occur. Consequently, the likelihood of the relationship's survival increases and, under certain parameters, the resulting gains in the surplus outweighs the loss due to the use of the inefficient rigid action. Also, recall that if the rigid action has not yet been used in the past, there is an additional cost of using it as it reduces the surplus in the relationship even after the shock passes. Hence, the optimal contract is more likely to call for a "precautionary" use of the rigid action when it has already been in place.

The second part of Proposition 4 states that the relationship becomes more fragile following the introduction of the standardized procedure. A relationship that starts with the agent taking the adaptive action may move more quickly towards the phase where the rigid action is used when the agent is already aware of the rigid action than when he is not.

The argument, again, relies on the fact that even if the relationship may recover after reaching Phase 2 (i.e., the agent can be induced to take the adaptive action), it becomes less valuable to the principal (i.e., $\bar{\pi}_r < \bar{\pi}$) as the rigid action remains available to the agent. Consequently, it is less resilient to shocks, and more likely to rely on the rigid action when the shocks arise in the future. In other words, by establishing the standardized procedure in the face of liquidity shocks, the principal can better weather the shock at present (and may save the relationship from termination), but it fundamentally changes the nature of the relationship in the future. Over time, the relationship becomes more reliant on the standardized work process even as it strives to foster worker initiative.

6. DISCUSSION AND CONCLUSION

The events of the past play a significant role in shaping an organization's future. In his seminal treatise on the limits of organization, Arrow (1974; p. 49) observes that "...the combination of uncertainty, indivisibility, and capital intensity associated with information channels and their use imply (a) that the actual structure and behavior of an organization may depend heavily upon random events, in other words on history, and (b) the very pursuit of efficiency may lead to rigidity and unresponsiveness to further change." Our analysis highlights a novel mechanism that speaks to this observation.

We show how the extent of worker initiative within a firm may evolve over time in response to private shocks to the firm's credibility. In a time of a crisis, a firm may avoid collapse by

reducing employee discretion and asking the workers to follow a set of rules that standardize the work processes. The implementation of such rules creates rigidities and compromises production. However, it is easier to incentivize the workers to adhere to a set of rules than to take initiative and adapt their actions to the underlying circumstances.

But the use of rules is a double-edged sword. While it can help a firm weather shocks in the short term, it may change the nature of the employment relationship in the long term. When a new rule is put in place, the workers learn what compromises may be acceptable to the principal, and it becomes more difficult to motivate the workers to exert consummate effort when discretion is given back to them. As the moral hazard problem aggravates, the value of the relationship decreases, making the firm more vulnerable to future shocks and more reliant on the use of rules.

We conclude with the following remarks. First, we focus on a parameter range where the firm may oscillate between periods of standardized work processes and encouragement of worker initiative. The standardized processes are used in the times of crisis, but after surviving the crisis the worker is again urged to take initiative. Thus, our result suggests that the process through which the firm becomes more rigid over time need not be “linear,” and it may go through multiple cycles where the emphasis shifts from initiative to rules and vice versa. This feature of the optimal contract aligns well with the pattern of fluctuation between the centralized and decentralized modes of organization that is frequently observed in the reality.⁷

However, one can consider parameters in our model (by relaxing Assumption 1 (iii)) where the relationship is stuck with standardized processes once they are made available. In particular, when the value of the output is too low or the agent’s rents under the adaptive action are too high (e.g., y is small and p is large), the maximum bonus the principal can credibly promise would no longer be enough to induce the agent to take the adaptive action when the rigid action is already available. This scenario reflects the so-called “structural inertia” in firms where they appear incapable of making significant changes to their organizational strategies in the face of changing business environments (Hannan and Freeman, 1989).

Second, our model does not consider the issue of heterogeneity in workers’ productivity. In reality, workers may vary in their innate abilities, and the low-ability workers may need more guidance on how to perform their jobs. If rules are conceived as a set of guidelines that minimize the risk of failure in a given job, then rules may increase the productivity of the low-ability workers by offering them a standardized work process. As a result, a firm with

⁷Nickerson and Zenger (2002) discusses several examples of fluctuations between centralization and decentralization including the case of Hewlett-Packard discussed earlier. Such fluctuations are often described as “time-honored” cycles due to their prevalence across industries and over time (Eccles and Nohria, 1992).

a set of heterogeneous workers might be more prone to rely on rules. However, as in our model, the incentives of the high-ability workers may still be negatively affected, and the same trade-off with rules that we highlight in the paper is likely to emerge.

Finally, in our model, the firm and the worker always have a common understanding of what is expected out of the worker. This is a natural assumption when rules are in place. As mentioned above, rules can serve as guidelines to the worker on how to do his job. In absence of rules however, this assumption becomes more important. When the worker initiative is desired, it is necessary that the worker understands what the firm's objectives are and what the worker needs to do in order to attain those objectives. In a complex production environment, it is conceivable that this understanding is difficult to establish, leading to a "problem of clarity" (Gibbons and Henderson, 2012a, 2012b). Thus, the strength of relational incentives depends not only on the extent of trust between the contracting parties but also on their ability to communicate clear expectations about their respective roles in the relationship. The interplay between the problems of "credibility" and "clarity" can have important implications for the optimal use of rules in relational contracts. A formal treatment of this issue is beyond the scope of this paper, and we leave it for future research.

APPENDIX

This appendix contains the proofs omitted in the text.

Proof of Lemma 1. Part (i) follows from standard arguments (as in Abreu et al. 1990) since the action space for each player in the stage game is finite. Part (ii) immediately follows from the availability of the public randomization device. The argument for part (iii) is given as follows.

Notice that it is sufficient to show this property for a payoff supported by a pure action. Without loss of generality, assume that $(\pi, u) = (\pi, U_r(\pi))$ and it is supported by the adaptive action ($a = A$), and the continuation payoffs (in the shock and no-shock states) are (π_s^A, u_s^A) and (π_n^A, u_n^A) . Suppose that $u_n^A < U_r(\pi_n^A)$. Now consider an alternative strategy that also specifies $a = A$ and offers continuation payoffs (π_s^A, u_s^A) and $(\pi_n^A, u_n^A + \varepsilon)$ where $\varepsilon > 0$ and $u_n^A + \varepsilon < U_r(\pi_n^A)$. Under this strategy, (PK_A^A) and (PK_P^A) imply that the principal's payoff remains at π whereas the agent's payoff is $u + (1 - \theta)\delta\varepsilon > U_r(\pi)$. It is routine to check that this strategy profile also satisfies all other constraints, and hence, constitutes a PPE. But this observation contradicts the fact that u is the highest PPE payoff to the agent when the principal's payoff is π (as we have assumed that (π, u) is on the frontier

U_r). Hence, we must have $u_n^A = U_r(\pi_n^A)$. An identical argument holds in the case of all other continuation payoffs. ■

Proof of Lemma 2. Part (i): Step 1. We claim that without loss of generality, we can assume that (TT^A) binds. We prove this by contradiction. Given a strategy profile where (TT^A) is slack, consider a new strategy where π_n^A is reduced by $\theta\varepsilon$ ($\varepsilon > 0$) and π_s^A is increased by $(1 - \theta)\varepsilon$, and all other aspects of the initial strategy profile are kept unchanged. Now, for ε sufficiently small, this new strategy satisfies all constraints that a PPE payoff must abide by when it is supported by the adaptive action, and yields a payoff (π, \hat{u}) where $\hat{u} \geq u$. To see this, note that as $b^A \geq 0$, we have $\pi_n^A > \pi_s^A$ (as (TT^A) is slack). So, as U_r is concave, for ε sufficiently small we have

$$\theta U_r(\pi_s^A + (1 - \theta)\varepsilon) + (1 - \theta)U_r(\pi_n^A - \theta\varepsilon) \geq \theta U_r(\pi_s^A) + (1 - \theta)U_r(\pi_n^A).$$

From Lemma 1 we know that the continuation payoffs are always on the frontier U_r . Hence, (PK_A^A) implies that under the new strategy profile the agent's payoff $\hat{u} \geq u$. By construction, (PK_P^A) remains unaltered; so (π, \hat{u}) satisfies (IR) and (IC^A) is (weakly) relaxed. Also by construction, (NN^A) is unaffected, and (TT^A) continues to hold as it was slack to begin with. Finally, as $\pi_n^A > \pi_s^A$ and since the PPE payoff set \mathcal{E}_r is convex, both $(\pi_s^A + (1 - \theta)\varepsilon, U_r(\pi_s^A + (1 - \theta)\varepsilon))$ and $(\pi_n^A - \theta\varepsilon, U_r(\pi_n^A - \theta\varepsilon))$ are in \mathcal{E}_r . So, (SE^A) holds. Hence, if (TT^A) is slack, either (π, u) is not on the frontier of \mathcal{E}_r , which is a contradiction, or one can construct a PPE where (TT^A) binds and the players get the exact same payoff as before.

Step 2. Given that (TT^A) binds, we have from (PK_P^A) that

$$\begin{aligned} \pi &= \theta [(1 - \delta)y + \delta\pi_s^A] + (1 - \theta) [(1 - \delta)(y - b^A) + \delta\pi_n^A] \\ &= (1 - \delta)y + \delta\pi_s^A. \end{aligned}$$

This gives that

$$(A1) \quad \pi_s^A = \frac{1}{\delta} (\pi - (1 - \delta)y).$$

As $\pi < y$ (note that the highest surplus that can be attained in a stage game is $y - C$), $\pi_s^A < \pi$.

Step 3. Next, we determine π_n^A . As (π, u) is on the frontier of \mathcal{E}_r and is supported by $a = A$, we have $u = u_r^A(\pi)$. Moreover, $\pi + u_r^A(\pi)$ is the maximum joint payoff attainable in any PPE that uses the adaptive action in the current period and gives a payoff of π to the principal. From Lemma 1 we know that the continuation payoffs are on the frontier, and Step 1 and

2 of this proof show that in any such PPE, we can assume that (TT^A) binds and π_s^A is constant (given π). Hence, we must have

$$\begin{aligned} \pi + u_r^A(\pi) &= \max_{b^A, \tilde{\pi}_n^A} (1 - \delta)(y - C) + \delta [\theta (\pi_s^A + U_r(\pi_s^A)) + (1 - \theta) (\tilde{\pi}_n^A + U_r(\tilde{\pi}_n^A))] \\ \text{s.t. } \theta [(1 - \delta)(-c) + \delta U_r(\pi_s^A)] + (1 - \theta) [(1 - \delta)(b^A - c) + \delta U_r(\tilde{\pi}_n^A)] &\geq u^* && (IC^A) \\ - (1 - \delta)b^A + \delta \tilde{\pi}_n^A &= \delta \pi_s^A && (TT^A) \\ b^A &\geq 0 && (NN^A) \\ 0 &\leq \tilde{\pi}_n^A \leq \bar{\pi}_r, && (SE^A) \end{aligned}$$

and the solution to the above program yields $\pi_n^A(\pi)$. Define

$$\bar{\pi}_r^* =: \sup\{\pi : U_{r-}'(\pi) \geq -1\}.$$

Below, we show that $\pi_n^A(\pi) = \bar{\pi}_r^* = \bar{\pi}_r$.

Step 4. First, we show that $\bar{\pi}_r^* = \bar{\pi}_r$. Suppose to the contrary that $\bar{\pi}_r^* < \bar{\pi}_r$. First note that $(\bar{\pi}_r^*, U_r(\bar{\pi}_r^*))$ is an extreme point and is therefore sustained by a pure action. Notice that it cannot be sustained by O . If so, then the associated continuation payoffs would be $(\bar{\pi}_r^*/\delta, U_r(\bar{\pi}_r^*)/\delta) \gg (\bar{\pi}_r^*, U_r(\bar{\pi}_r^*))$, and it contradicts the definition of $\bar{\pi}_r^*$. Hence, $(\bar{\pi}_r^*, U_r(\bar{\pi}_r^*))$ is sustained either by A or R .

Step 5. Suppose that $(\bar{\pi}_r^*, U_r(\bar{\pi}_r^*))$ is sustained by A . Since (TT^A) binds, we have

$$\pi_s^A(\bar{\pi}_r^*) = (\bar{\pi}_r^* - (1 - \delta)y) / \delta < \bar{\pi}_r^*.$$

Step 5a: Now, if $b^A = 0$, from (TT^A) we have $\pi_n^A(\bar{\pi}_r^*) = \pi_s^A(\bar{\pi}_r^*)$. Consider in this case a perturbation in which $\tilde{\pi}_s^A = \tilde{\pi}_n^A = \pi_s^A(\bar{\pi}_r^*) + \varepsilon$, and b^A unchanged. This perturbation satisfies all the constraints. It increases the payoff of the principal by $\delta\varepsilon$ and changes the agent's payoff by

$$\delta (U_r(\pi_s^A(\bar{\pi}_r^*) + \varepsilon) - U_r(\pi_s^A(\bar{\pi}_r^*))) \geq -\delta\varepsilon,$$

where the inequality follows as U_r is concave and $\pi_s^A(\bar{\pi}_r^*) < \bar{\pi}_r^*$. But this implies (along with concavity of U_r) that $U_r(\bar{\pi}_r^* + \varepsilon\delta) \geq U_r(\bar{\pi}_r^*) - \varepsilon\delta$, contradicting the definition of $\bar{\pi}_r^*$.

Step 5b: Next, if $b^A > 0$, we then consider a perturbation in which $\tilde{\pi}_s^A = \pi_s^A(\bar{\pi}_r^*) + (1 - \delta)\varepsilon$, $\tilde{b} = b^A(\bar{\pi}_r^*) - \delta\varepsilon$ and $\pi_n^A(\bar{\pi}_r^*)$ unchanged. This perturbation again satisfies all the constraints. It increases the payoff of the principal by $(1 - \delta)\delta\varepsilon$ and changes the agent's payoff by

$$\theta\delta (U_r(\pi_s^A(\bar{\pi}_r^*) + (1 - \delta)\varepsilon) - U_r(\pi_s^A(\bar{\pi}_r^*))) - (1 - \theta)\delta(1 - \delta)\varepsilon \geq -\delta(1 - \delta)\varepsilon.$$

The inequality again follows because U_r is concave and $\pi_s^A(\bar{\pi}_r^*) < \bar{\pi}_r^*$. And this again implies that $U_r(\bar{\pi}_r^* + \varepsilon\delta(1 - \delta)) \geq U_r(\bar{\pi}_r^*) - \varepsilon\delta(1 - \delta)$, contradicting the definition of $\bar{\pi}_r^*$.

Step 6. Next, suppose that $(\bar{\pi}_r^*, U_r(\bar{\pi}_r^*))$ is sustained by R . In this case, if $b^R > 0$ or if $b^R = 0$ and $\pi_n^A(\bar{\pi}_r^*) = \pi_s^A(\bar{\pi}_r^*) < \bar{\pi}_r^*$, the same perturbations as described above lead to contradictions. It remains to derive contradiction for $b^R = 0$ and $\pi_n^R(\bar{\pi}_r^*) = \pi_s^R(\bar{\pi}_r^*) \geq \bar{\pi}_r^*$. Notice that if $\pi_n^R(\bar{\pi}_r^*) = \pi_s^R(\bar{\pi}_r^*) = \bar{\pi}_r^*$, we then have $U_r(\bar{\pi}_r^*) = -c$, which is impossible. If $\pi_n^R(\bar{\pi}_r^*) = \pi_s^R(\bar{\pi}_r^*) > \bar{\pi}_r^*$, consider a deviation where $\tilde{\pi}_s^R = \tilde{\pi}_n^R = \pi_s^R(\bar{\pi}_r^*) - \varepsilon$, and b^R remain to be 0. This perturbation satisfies all the constraints. It decreases the payoff of the principal by $\delta\varepsilon$ and increases the agent's payoff by

$$\delta (U_r(\pi_s^A(\bar{\pi}_r^*) - \varepsilon) - U_r(\pi_s^A(\bar{\pi}_r^*))) > \delta\varepsilon,$$

where the strict inequality follow from the definition of $\bar{\pi}_r^*$ and that both $\pi_s^A(\bar{\pi}_r^*) > \bar{\pi}_r^*$ and U_r is concave. But this implies $U'_{r-}(\bar{\pi}_r^*) < -1$, which is a contradiction. This finishes showing that $\bar{\pi}_r^* = \bar{\pi}_r$ so that $U'_{r-}(\pi) \geq -1$ for all π .

Step 7. Given that $U'_{r-}(\pi) \geq -1$ for all π , it is then without loss of generality to choose $\pi_n^A(\pi) = \bar{\pi}_r$. To see this, suppose to the contrary that $\pi_n^A(\pi) < \bar{\pi}_r$. Now consider an alternative profile where $\tilde{\pi}_n^A = \pi_n^A(\pi) + (1 - \delta)\varepsilon$ and $\tilde{b}^A = b^A + \delta\varepsilon$. Under this perturbation, the principal's payoff is preserved and so are all the constraints. The agent's payoff changes by

$$\delta (U_r(\pi_n^A(\pi) + (1 - \delta)\varepsilon) - U_r(\pi_n^A(\pi))) + (1 - \delta)\delta\varepsilon \geq 0,$$

where the inequality holds because $U'_{r-}(\pi) \geq -1$ for all π . This implies that this perturbation yields a payoff that is also on the payoff frontier (U_r), and therefore, we can keep increase $\pi_n^A(\pi)$ (adjusting b^A accordingly) until $\pi_n^A(\pi) = \bar{\pi}_r$.

Step 8. Finally, we show that $U'_{r-}(\pi) > -1$ for all π , so the choice of $\pi_n^A(\pi)$ is unique. To see this, suppose to the contrary that there exists a $\pi^* < \bar{\pi}_r$ where $U'_{r-}(\pi) = -1$ for $\pi \in [\pi^*, \bar{\pi}_r]$, where π^* is the left end point of this line segment. Notice that $(\pi^*, U(\pi^*))$ is an extreme point, and Assumption 1 ensures that this point is sustained by A . Now (TT^A) again implies that $\pi_s^A(\pi^*) < \pi^*$. Also note that

$$b^A(\pi^*) = y - (\pi^* - \delta\bar{\pi}_r) / (1 - \delta) > y - (\bar{\pi}_r - \delta\bar{\pi}_r) / (1 - \delta) > 0.$$

Now consider the following perturbation: decrease $b^A(\pi^*)$ by $\delta\varepsilon$, increase $\pi_s^A(\pi^*)$ by $(1 - \delta)\varepsilon$ and keep the rest unchanged. Under this perturbation, all constraints are satisfied. The principal's payoff increases by $\delta(1 - \delta)\varepsilon$. The agent's payoff changes by

$$\theta\delta (U_r(\pi_s^A(\pi^*) + (1 - \delta)\varepsilon) - U_r(\pi_s^A(\pi^*))) - (1 - \theta)(1 - \delta)\delta\varepsilon > -\delta(1 - \delta)\varepsilon,$$

implying that this perturbation generates a payoff that exceeds $U_r(\pi^* + \delta(1 - \delta)\varepsilon)$. This is a contradiction. This implies that we must have $\pi_n^A(\pi) = \bar{\pi}_r$.

Step 9. As (TT^A) binds, $(A1)$ implies

$$b^A = y - \frac{\pi - \delta \bar{\pi}_r}{1 - \delta}.$$

This observation completes the proof of Part (i).

Part (ii): The proof is identical to that of Part (i). As above, we may assume that (TT^R) binds with equality; and thus, (PK_P^R) implies

$$\pi = (1 - \delta)py + \delta\pi_s^R.$$

This gives that

$$(A2) \quad \pi_s^R = \frac{1}{\delta}(\pi - (1 - \delta)py).$$

Next, because $U'_{r-}(\pi) > -1$ for all π , the same argument as above gives that

$$\pi_n^R = \bar{\pi}_r.$$

Now, the formula for b^R follows from (TT^A) .

Part (iii): Immediate from (PK^O) . ■

In order to prove Proposition 1, we first prove the following lemma.

Lemma 6. $U_r(0) = 0$ and $(0, 0)$ is sustained by $a = O$. Furthermore, if for some $\tilde{\pi} > 0$, $(\tilde{\pi}, U_r(\tilde{\pi}))$ is sustained by $a = O$, then for all $\pi \leq \tilde{\pi}$, $U_r(\pi) = u_r^O(\pi)$. Hence, there exists a cutoff π_r^O such that U_r is a straight line between $(0, 0)$ and $(\pi_r^O, U_r(\pi_r^O))$, and $U_r(\pi) = u_r^O(\pi)$ if and only if $\pi \leq \delta\pi_r^O$.

Proof. Step 1. As $(0, U_r(0))$ is an extreme point, it must be sustained by a pure action. But it is routine to check that $(0, U_r(0))$ cannot be sustained by $a = A$ or R , as the promise-keeping and truth-telling constraints cannot be satisfied simultaneously. As only $a = O$ is feasible, from (PK^O) we have $\pi^O = 0$. So, the unique PPE that supports $(0, U_r(0))$ is one where both players take their outside options in all periods. Hence, $(0, U_r(0)) = (0, 0)$.

Step 2. From Lemma 1 and (PK^O) we have

$$u_r^O(\pi) = \delta U_r(\pi^O(\pi)) = \delta U_r(\pi/\delta)$$

for all $\pi \in [0, \delta\tilde{\pi}_r]$ (i.e., for all π where $u_r^O(\pi)$ is well-defined). Hence,

$$u'_{r-}(\pi) = U'_{r-}(\pi/\delta) \leq U'_{r-}(\pi)$$

for all $\pi \in (0, \delta\bar{\pi}_r)$, where the inequality follows from the concavity of U_r (notice that by virtue of being concave, the left- and right-derivative of U_r always exist in the interior of its domain). But as $u_r^O(\tilde{\pi}) = U_r(\tilde{\pi})$, this implies that $u_r^O(\pi) \geq U_r(\pi)$ for all $\pi \leq \tilde{\pi}$. But as $U_r(\pi) \geq u_r^O(\pi)$, we have $U_r(\pi) = u_r^O(\pi)$ for all $\pi \leq \tilde{\pi}$.

Step 3. As $U_r(\pi) = u_r^O(\pi)$ for all $\pi \leq \tilde{\pi}$, we have $U'_{r-}(\pi) = u'_{r-}(\pi)$. So, from step 2 above, $u'_{r-}(\pi) = U'_{r-}(\pi/\delta) = U'_{r-}(\pi)$, and since U_r is concave, this implies that U_r is a straight line passing through $(0, 0)$ and extends at least up to the point $(\tilde{\pi}, U_r(\tilde{\pi}))$. Denote the right-most end-point of this line as $(\pi_r^O, U_r(\pi_r^O))$.

Step 4. Take any $(\pi, U_r(\pi))$ such that $\pi/\delta \leq \pi_r^O$. We claim that such a payoff is sustainable by $a = O$. Note that the associated continuation payoffs $(\pi^O, u^O) = (\pi/\delta, U_r(\pi/\delta))$ (using Lemma 1 and (PK^O)), and hence, (SE^O) is satisfied. Finally, (PK^O) for the agent holds as $U_r(\pi) = \delta U_r(\pi/\delta)$ since U_r is linear.

Step 5. But if $\pi/\delta > \pi_r^O$, then the payoff $(\pi, U_r(\pi))$ cannot be sustained by $a = O$. The argument is as follows. If $\pi_r^O < \bar{\pi}_r$, we have

$$U_r(\pi) > (1 - \delta)U_r(0) + \delta U_r(\pi/\delta) = \delta U_r(\pi/\delta).$$

The inequality follows from the fact that $U_r(\pi')$ is concave and the segment starting from $(0, 0)$ is linear if only if $\pi' < \pi_r^O$ whereas $\pi/\delta > \pi_r^O$. Also the equality follows from $U_r(0) = 0$. But this implies that (PK^O) for the agent is violated, and hence, $(\pi, U_r(\pi))$ cannot be supported by $a = O$. And if $\pi_r^O = \bar{\pi}_r$, the proof is immediate as by (PK^O) any point sustained by $a = O$ requires $\pi^O(\pi) = \pi/\delta \leq \bar{\pi}_r = \pi_r^O$. ■

Lemma 7. *Both the rigid and the adaptive action are used on the payoff frontier. In particular, $\pi_r^O < \bar{\pi}_r$, and $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ is sustained by the adaptive action whereas $(\pi_r^O, U_r(\pi_r^O))$ is sustained by the rigid action.*

Proof. First, consider the case of the *adaptive action*. We prove this by constructing a stationary PPE with associated payoffs (π^*, u^*) where $\pi^* > py$ (though the payoffs need not be on the frontier). As py is an upper bound on the principal's payoff in any PPE where the adaptive action is never used, the adaptive action must be used on the payoff frontier. The proof is given by the following steps.

Step A1. Consider the following stationary strategy profile where in each period, the agent chooses the adaptive action, receives a bonus of $b^* \geq 0$ in the no-shock state and gets a payoff

of $u^* = \frac{1-\delta}{1-p}(pC - c)$. When the principal claims that it is a shock state, the relationship terminates. Denote the principal's associated payoff as π^* . For this strategy profile to be a PPE, (π^*, u^*) must satisfy all constraints given in Section 3.1 for the case of adaptive action. Note that (IC^A) and (IR) for the agent are trivially satisfied when $u = u^*$. Also notice that the (NR) constraint in this case is the same as (TT^A) . Hence, it remains to check if the following constraints are satisfied:

$$\begin{aligned} u^* &= (1-\delta)(-C) + (1-\theta)((1-\delta)b^* + \delta u^*), & (PK_A^A) \\ \pi^* &= (1-\delta)y + (1-\theta)(-(1-\delta)b^* + \delta\pi^*), & (PK_P^A) \\ &-(1-\delta)b^* + \delta\pi^* \geq 0, & (TT^A) \\ &\pi^* \geq 0. & (IR) \end{aligned}$$

Since the proposed strategy profile is stationary, if (π^*, u^*) satisfies the above constraints, it also satisfies (SE^A) .

Step A2. From (PK_A^A) , we obtain

$$(A3) \quad (1-\theta)b^* = C + \frac{1-(1-\theta)\delta}{1-\delta}u^* =: K.$$

And using (PK_A^A) and (PK_P^A) we have

$$\pi^* + u^* = (1-\delta)(y - C) + (1-\theta)(\delta u^* + \delta\pi^*).$$

Hence,

$$(A4) \quad \pi^* = \frac{(1-\delta)(y - C)}{1 - (1-\theta)\delta} - u^* = \frac{(1-\delta)(y - K)}{1 - (1-\theta)\delta}.$$

Step A3. We claim that u^* , b^* as given in (A3), and π^* as given in (A4) satisfy all four constraints given above. Trivially (PK_A^A) and (PK_P^A) are satisfied by construction. To see that (TT^A) holds (and hence (IR) holds as well), note that using (A3) and (A4), (TT^A) can be written as

$$\frac{\delta(1-\delta)(y - K)}{1 - (1-\theta)\delta} \geq (1-\delta)b^* \Leftrightarrow y \geq \frac{K}{(1-\theta)\delta}.$$

But this is true by Assumption 1 (iii). Hence, the above strategy profile constitutes a PPE.

Step A4. Finally, we have $\pi^* > py$ as using (A4) it boils down to

$$((1-\delta)(1-p) - p\theta\delta)y > (1-\delta)K,$$

which is the case by Assumption 1 (iii). But this implies that $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ must be supported by adaptive action. Notice that as $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ is an extreme point, it must be sustained by a pure action. But it cannot be sustained by $a = O$, as then by Lemma 2 we have

$$\pi^O(\bar{\pi}_r) = \frac{1}{\delta} \bar{\pi}_r > \bar{\pi}_r,$$

which is a contradiction. Also, if $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ is sustained by $a = R$ instead, we have

$$\pi_s^R(\bar{\pi}_r) = \frac{1}{\delta} (\bar{\pi}_r - (1 - \delta)py) > \bar{\pi}_r,$$

(the last inequality follows because $\bar{\pi}_r \geq \pi^* > py$) and this is a contradiction as well.

Next, consider the case of the *rigid action*. The proof is given by the following steps (the reader may note that the steps R1 and R2 below are more elaborate than what is necessary for this proof, but we adopt this approach as it remains applicable for the proof of Lemma 9 below, and hence, it allows us to avoid repetition).

Step R1. Suppose to the contrary that rigid action is not used. So by Lemma 6, it follows that $(\pi_r^O, U_r(\pi_r^O))$ must be sustained by the adaptive action, and hence, $u_r^A(\pi_r^O) = U_r(\pi_r^O)$. Let s be the slope between $(0, 0)$ and $(\pi_r^O, U_r(\pi_r^O))$. As $\pi_s^A(\pi_r^O) < \pi_r^O$, by APS bang-bang result and Lemma 6 we have $\pi_s^A(\pi_r^O) = 0$ as $(0, 0)$ is the only extreme point to the left of π_r^O . Hence, we have $\pi_r^O = (1 - \delta)y$, and therefore,

$$s := \frac{U_r((1 - \delta)y)}{(1 - \delta)y}.$$

Furthermore, from (PK_A^A) and (PK_P^A) (and using the fact that $\pi_s^A(\pi_r^O) = 0$ and $\pi_n^A(\pi) = \bar{\pi}_r$) we have

$$\begin{aligned} U_r((1 - \delta)y) &= -(1 - \delta)C + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)) \\ &\leq -(1 - \delta)C + (1 - \theta)\delta(y - C), \end{aligned}$$

where the inequality follows because $y - C$ is the aggregate surplus under efficiency. So,

$$s \leq \frac{-(1 - \delta)C + (1 - \theta)\delta(y - C)}{(1 - \delta)y}.$$

Step R2. Next, consider a strategy profile where the agent chooses the rigid action, bonus payment is b^R as given in Lemma 2, and the continuation payoffs following shock and no-shock states are $(0, 0)$ and $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ respectively. Under this strategy profile, the principal's payoff is $(1 - \delta)py$ (from (A2)), and the agent's payoff $u = u_r^R((1 - \delta)py)$ satisfies

$$u_r^R((1 - \delta)py) + (1 - \delta)py = (1 - \delta)(py - c) + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)).$$

It follows that

$$S := \frac{u_r^R((1-\delta)py)}{(1-\delta)py} = \frac{-(1-\delta)c + (1-\theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r))}{(1-\delta)py}.$$

Step R3. We claim that $S > s$. Since $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ is sustained by the adaptive action, we have $U_r(\bar{\pi}_r) \geq u^*$ (by (IC^A)). Also, by definition $\bar{\pi}_r \geq \pi^*$. Hence, using (A4) we obtain

$$\bar{\pi}_r + U_r(\bar{\pi}_r) \geq \pi^* + u^* = \frac{(1-\delta)(y-C)}{1-(1-\theta)\delta}.$$

So,

$$S \geq \frac{1}{(1-\delta)py} \left(-(1-\delta)c + \frac{(1-\theta)\delta(1-\delta)(y-C)}{1-(1-\theta)\delta} \right)$$

Now,

$$-(1-\delta)c + \frac{(1-\theta)\delta(1-\delta)(y-C)}{1-(1-\theta)\delta} > p(-(1-\delta)C + (1-\theta)\delta(y-C)),$$

as it can be rearranged as

$$(1-\delta)(pC - c) + \frac{(1-\theta)\delta(y-C)}{1-(1-\theta)\delta} ((1-\delta)(1-p) - p\delta\theta) > 0,$$

which is the case by Assumption 1 (ii) and (iii).

Step R4. As $S > s$ we have

$$\frac{u_r^R((1-\delta)py)}{(1-\delta)py} > \frac{U_r((1-\delta)y)}{(1-\delta)y} = \frac{U_r((1-\delta)py)}{(1-\delta)py}$$

(recall that U_r is a straight line between $(0, 0)$ and $(\pi_r^O, U_r(\pi_r^O))$, and $(1-\delta)py < (1-\delta)y \leq \pi_r^O$). But this implies

$$u_r^R((1-\delta)py) > U_r((1-\delta)py),$$

which is a contradiction. Therefore, $(\pi_r^O, U_r(\pi_r^O))$ must be sustained by the rigid action.

Notice that as $\pi_r^O \leq \bar{\pi}_r$ and $\bar{\pi}_r$ can only be sustained by the adaptive action whereas π_r^O can only be sustained by the rigid action, we have $\pi_r^O \neq \bar{\pi}_r$. Hence, $\pi_r^O < \bar{\pi}_r$. ■

Lemma 8. *If $u_r^A(\pi') \geq u_r^R(\pi')$ for some π' , then $u_r^A(\pi) \geq u_r^R(\pi)$ for all $\pi \geq \pi'$.*

Proof. Adding (PK_P^A) and (PK_A^A) we obtain that

$$\pi + u_r^A(\pi) = (1 - \delta)(y - C) + \theta\delta(\pi_s^A + U_r(\pi_s^A)) + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)),$$

where

$$\pi_s^A = \frac{1}{\delta}(\pi - (1 - \delta)y).$$

Similarly, adding (PK_P^R) and (PK_A^R) we obtain that

$$\pi + u_r^R(\pi) = (1 - \delta)(py - c) + \theta\delta(\pi_s^R + U_r(\pi_s^R)) + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)),$$

where

$$\pi_s^R = \frac{1}{\delta}(\pi - (1 - \delta)py).$$

This implies that

$$\begin{aligned} u_r^A(\pi) - u_r^R(\pi) &= (1 - \delta)((1 - p)y - C + c) + \theta\delta(\pi_s^A + U_r(\pi_s^A)) - \theta\delta(\pi_s^R + U_r(\pi_s^R)) \\ &= (1 - \delta)[(1 - p)y(1 - \theta) - C + c] + \theta\delta(U_r(\pi_s^A) - U_r(\pi_s^R)). \end{aligned}$$

As a result,

$$u_{r+}^{A'}(\pi) - u_{r+}^{R'}(\pi) = \theta(U_r'(\pi_s^A) - U_r'(\pi_s^R)) \geq 0$$

since $\pi_s^A = \frac{1}{\delta}(\pi - (1 - \delta)y) < \frac{1}{\delta}(\pi - (1 - \delta)py) = \pi_s^R$ and U_r is concave. In other words, if $u_r^A(\pi') \geq u_r^R(\pi')$ for some π' , then $u_r^A(\pi) \geq u_r^R(\pi)$ for all $\pi \geq \pi'$. ■

Proof of Proposition 1. Part (i): That $U_r(0) = 0$, the existence π_r^O , and the linearity of U_r between $(0, 0)$ and $(\pi_r^O, U_r(\pi_r^O))$ are proved in Lemma 6. By virtue of linearity, any payoff in this line segment can be supported by randomization between the two end points. Hence, without loss of generality, we can also assume that $a = O$ is played on the frontier only to support $(0, 0)$ payoff.

For expositional clarity, below we prove parts (ii) and (iv) first, and then prove part (iii).

Part (ii) and Part (iv): Recall from Lemma 7 (step R3) that $(\pi_r^O, U_r(\pi_r^O))$ is supported by $a = R$ and that $\pi < \pi_r^O$ is supported by randomization (by Part (i) above). Lemma 7 also shows that the adaptive action is used on the frontier, and Lemma 8 implies (along with the fact that $u_r^A(\pi)$ and $u_r^R(\pi)$ are concave functions) that the set of π values such that $(\pi, U_r(\pi))$ is supported by each of these two actions ($a = A$ and R) are intervals (potentially containing a single point only) on $[0, \bar{\pi}_r]$. Moreover, if $(\pi, U_r(\pi))$ is supported by $a = R$ and $(\pi', U_r(\pi'))$ is supported by $a = A$, then it must be that $\pi' > \pi$. Hence, there exists two cutoffs π_r^R and π_r^A where $\pi_r^O \leq \pi_r^R \leq \pi_r^A \leq \bar{\pi}_r$ (but $\pi_r^O < \bar{\pi}_r$) such that $(\pi, U_r(\pi))$ is supported by $a = R$ for $\pi \in [\pi_r^O, \pi_r^R]$ and by $a = A$ for $\pi \in [\pi_r^A, \bar{\pi}_r]$.

It remains to show that $U_r(\bar{\pi}_r) = u^*$. Suppose on the contrary $U_r(\bar{\pi}_r) > u^*$ (from (IC^A) we must have $U_r(\bar{\pi}_r) \geq u^*$). Since $(\bar{\pi}_r, U_r(\bar{\pi}_r))$ is supported by $a = A$, by Lemma 7, we know that the associated continuation payoffs for the principal in the shock and no-shock states are $\pi_s^A < \bar{\pi}_r$ and $\bar{\pi}_r$, respectively. And the associated bonus payment $b^A = y - \bar{\pi}_r > 0$ as $y - C$ is an upper bound on $\bar{\pi}_r$. Now, consider an alternate strategy profile where the agent is asked choose A , the principal's continuation payoffs in the shock and no-shock states are $\hat{\pi}_s^A = \pi_s^A + \varepsilon$ and $\bar{\pi}_r$, respectively, and the bonus is $\hat{b}^A = b^A - \delta\varepsilon/(1 - \delta)$ where $\varepsilon > 0$. From (PK_A^A) and (PK_P^A) we obtain the associated payoffs as

$$\hat{u} = \theta [(1 - \delta)(-C) + \delta U_r(\pi_s^A + \varepsilon)] + (1 - \theta) [(1 - \delta)(b^A - \delta\varepsilon/(1 - \delta) - C) + \delta U_r(\bar{\pi}_r)]$$

and

$$\hat{\pi} = \theta [(1 - \delta)y + \delta(\pi_s^A + \varepsilon)] + (1 - \theta) [(1 - \delta)(y - b^A + \delta\varepsilon/(1 - \delta)) + \delta\bar{\pi}_r]$$

Observe that under the new strategy profile (NR^A) is relaxed, (TT^A) remains unaltered by construction. Moreover, for ε sufficiently small, both (IC^A) and (NN^A) remain slack (i.e., $\hat{u} > u^*$ and $\hat{b}^A > 0$), and $\hat{\pi}_s^A < \bar{\pi}_r$ so that (SE^A) is satisfied as well. Hence, the proposed strategy profile constitutes a PPE where the principal's payoff is $\hat{\pi} = \bar{\pi}_r + \delta\varepsilon > \bar{\pi}_r$, which is a contradiction.

Part (iii): If $\pi_r^R < \pi_r^A$, it implies that any payoff $(\pi, U(\pi))$ where $\pi \in [\pi_r^R, \pi_r^A]$ cannot be supported by any of the three pure actions. But such $(\pi, U(\pi)) \in \mathcal{E}_r$ as \mathcal{E}_r is convex. So, $(\pi, U(\pi))$ must be supported by randomization between a payoff that is supported by $a = R$ and one that is supported by $a = A$. Consequently, $U_r(\pi)$ is linear on this interval. Also, it is without loss of generality to assume that we randomize between the end points $(\pi_r^R, U(\pi_r^R))$ and $(\pi_r^A, U(\pi_r^A))$. ■

In order to prove Proposition 2, we first prove the following lemma.

Lemma 9. *The PPE frontier U satisfies the following properties:*

(i) $U(0) = 0$ and if for some $\tilde{\pi} > 0$, $(\tilde{\pi}, U(\tilde{\pi}))$ is sustained by $a = \mathcal{O}$, then for all $\pi \leq \tilde{\pi}$, $U(\pi) = u^\mathcal{O}(\pi)$. Hence, there exists a cutoff $\pi^\mathcal{O}$ such that U is a straight line between $(0, 0)$ and $(\pi^\mathcal{O}, U(\pi^\mathcal{O}))$, and $U(\pi) = u^\mathcal{O}(\pi)$ if and only if $\pi \leq \delta\pi^\mathcal{O}$. Moreover, $\pi^\mathcal{O} = \pi_r^\mathcal{O} = (1 - \delta)py$.

(ii) $U(\bar{\pi}) = 0$, $\bar{\pi} > \bar{\pi}_r$, and $U'_-(\bar{\pi}) > -1$.

(iii) The adaptive action ($a = \mathcal{A}$) is used on U . Moreover, if $U(\pi') = u^{\mathcal{A}}(\pi')$ for some π' then $U(\pi) = u^{\mathcal{A}}(\pi)$ for all $\pi \geq \pi'$.

Proof. Part (i): To see that $\pi^O = \pi_r^O$, note that by the same argument as given in Lemma 7, π^O must be supported by $a = R$ (as is the case for π_r^O). Also, note that both U and U_r are straight lines where the left-most point is $(0, 0)$ in both cases, and the right-most points are $(\pi^O, U(\pi^O))$ and $(\pi_r^O, U(\pi_r^O))$, respectively. Hence, by APS bang-bang result, $\pi_s^R(\pi^O) = \pi_s^R(\pi_r^O) = 0$. But as $\pi_s^R(\pi) = \frac{1}{\delta}(\pi - (1 - \delta)py)$, we have $\pi^O = \pi_r^O = (1 - \delta)py$. The proof of all other statements of this part are identical to the proof of part (i) of Lemma 6.

Part (ii): The proof of $U(\bar{\pi}) = 0$ is similar to that of $U_r(\bar{\pi}_r) = u^*$ given above. To see that $\bar{\pi} > \bar{\pi}_r$, notice that $U(\pi) \geq U_r(\pi)$ and, hence, $\bar{\pi} \geq \bar{\pi}_r$ as the principal always has the option of revealing the rigid action at the beginning of the game. In addition, $U(\bar{\pi}_r) \geq U_r(\bar{\pi}_r) > U(\bar{\pi}) = 0$. So, it must be that $\bar{\pi} > \bar{\pi}_r$. Finally, it follows from the same argument as the proof of $U_r'(\pi) > -1$ (in Step 3 of the proof of Lemma 2 Part (i)) that $U'_-(\pi) > -1$. The details are omitted.

Part (iii): Since $\bar{\pi} > \bar{\pi}_r$, $(\bar{\pi}, U(\bar{\pi})) \notin \mathcal{E}_r$. Hence, it cannot be sustained by $a \in \{A, R, O\}$. Also, it cannot be sustained by $a = \mathcal{O}$ as the continuation payoff $\pi^O(\bar{\pi}) = \bar{\pi}/\delta$ is not feasible. Hence, it must be sustained by $a = \mathcal{A}$; in other words, $a = \mathcal{A}$ is used on U . Next, we show that if $(\pi', U(\pi'))$ is supported by \mathcal{A} for some π' , then $u^{\mathcal{A}}(\pi) \geq U_r(\pi)$ for all $\pi > \pi'$. This implies that $U(\pi) = u^{\mathcal{A}}(\pi)$ for all $\pi > \pi'$. The proof is given by the following steps.

Step 1. Let π_l be the smallest π such that $U(\pi) = u^{\mathcal{A}}(\pi)$ (π_l exists as both U and $u^{\mathcal{A}}$ are continuous). Notice that $\pi_l \geq (1 - \delta)y$ as $\pi_s^{\mathcal{A}}(\pi_l) \geq 0$. Now we first show that for all $\pi < \pi_l$, either $U(\pi) = U_r(\pi)$ or $U(\pi)$ is sustained by randomization. The argument is as follows. Since $(\pi, U(\pi))$ is not supported by $a = \mathcal{A}$, we have $U(\pi) > u^{\mathcal{A}}(\pi) \geq u_r^{\mathcal{A}}(\pi)$. Hence, $(\pi, U(\pi))$ is either supported by a pure action $a \in \{\mathcal{O}, O, R\}$ or by a randomization. But if $(\pi, U(\pi))$ is supported by any of these pure actions, it must be that $U(\pi) = U_r(\pi)$. Recall that $\pi^O = \pi_r^O = (1 - \delta)py$ and the actions \mathcal{O} and O are never used for any $\pi > \delta\pi^O$. Hence, for $\pi \in [0, (1 - \delta)py]$, $U(\pi) = U_r(\pi)$ as both are straight lines between $(0, 0)$ and $(\pi^O, u_r^R(\pi^O))$. Moreover, if $(\pi, U(\pi))$ is supported by $a = R$ for some $\pi \in ((1 - \delta)py, \pi_l]$, we trivially have $U(\pi) = U_r(\pi) = u^R(\pi)$.

Step 2. Next, we claim that for all $\pi < \pi_l$,

$$(A6) \quad \frac{d}{d\pi}U(\pi) \geq \frac{d}{d\pi}U_r(\pi).$$

This is trivially the case if for all $\pi < \pi_l$, $(\pi, U(\pi))$ is supported by a pure action $a \in \{\mathcal{O}, O, R\}$, and hence, $U(\pi) = U_r(\pi)$. Now suppose that $(\pi, U(\pi))$ is sustained by a randomization. Denote the left point of the randomization be π_L ; so, $U'(\pi) = U'(\pi_L)$. Moreover, we can argue that $U'(\pi_L) \geq U'_r(\pi_L)$. Since $(\pi_L, U(\pi_L))$ is supported by $a = R$, $u_r^R(\pi_L) = U(\pi_L)$. Also, $U(\pi_L) \geq U_r(\pi_L)$ (as the inequality holds for all π), and $U_r(\pi_L) \geq u_r^R(\pi_L)$ as U_r is the frontier when the rigid action is available. So, we obtain $U(\pi_L) = U_r(\pi_L)$, and the fact that $U(\pi) \geq U_r(\pi)$ for all π , implies $U'(\pi_L) \geq U'_r(\pi_L)$. But also note that $U'_r(\pi_L) \geq U'_r(\pi)$ as U_r is concave. Combining these observations we have $U'(\pi) = U'(\pi_L) \geq U'_r(\pi_L) \geq U'_r(\pi)$, as claimed in (A6).

Step 3. Now, suppose to the contrary that $u^A(\pi) < U_r(\pi)$ for some $\pi > \pi_l$. It follows that there exists some $\hat{\pi} \in (\pi_l, \pi)$ such that

$$\frac{d}{d\pi} u^A(\hat{\pi}) < \frac{d}{d\pi} U_r(\hat{\pi}),$$

where the derivative can be thought of as the right or left derivative (with the proper inequalities) when the derivative fails to exist. Let

$$D := \left\{ \pi : \frac{d}{d\pi} u^A(\pi) < \frac{d}{d\pi} U_r(\pi) \mid \pi \geq \pi_l \right\}.$$

Note that for any $\tilde{\pi} \in [\pi_L, \inf D)$, we have $u^A(\tilde{\pi}) = U(\tilde{\pi})$, and therefore,

$$\frac{d}{d\pi} u^A(\tilde{\pi}) = \frac{d}{d\pi} U(\tilde{\pi}).$$

Step 4. Take a $\pi_m \in D$ such that $\pi_s^A(\pi_m) < \inf D$. Since $\pi_m \in D$, we have

$$\frac{d}{d\pi} u^A(\pi_m) < \frac{d}{d\pi} U_r(\pi_m).$$

But since

$$\pi + u^A(\pi) = (1 - \delta)(y - C) + \delta [\theta (\pi_s^A(\pi) + U(\pi_s^A(\pi))) + (1 - \theta)(\bar{\pi} + U(\bar{\pi}))],$$

we have,

$$(A7) \quad \frac{d}{d\pi} u^A(\pi) = \theta \frac{d}{d\pi} U(\pi_s^A(\pi)) - (1 - \theta).$$

Similarly, for $a \in \{A, R\}$, we obtain

$$(A8) \quad \frac{d}{d\pi} u_r^a(\pi) = \theta \frac{d}{d\pi} U_r(\pi_s^a(\pi)) - (1 - \theta).$$

Using (A7) and (A8) along with the fact that $\pi_s^A(\pi) = \pi_s^A(\pi)$, we obtain:

$$\begin{aligned}
 \frac{d}{d\pi}U_r(\pi_m) &\leq \max\left\{\frac{d}{d\pi}u_r^A(\pi_m), \frac{d}{d\pi}u_r^R(\pi_m)\right\} \\
 &= \theta \max\left\{\frac{d}{d\pi}U_r(\pi_s^A(\pi_m)), \frac{d}{d\pi}U_r(\pi_s^R(\pi_m))\right\} - (1-\theta) \\
 &= \theta \frac{d}{d\pi}U_r(\pi_s^A(\pi_m)) - (1-\theta).
 \end{aligned}$$

The inequalities above then imply that

$$\frac{d}{d\pi}U(\pi_s^A(\pi_m)) < \frac{d}{d\pi}U_r(\pi_s^A(\pi_m)).$$

But this is a contradiction because if $\pi_s^A(\pi_m) \in [\pi_l, \inf D)$, we have

$$\frac{d}{d\pi}U(\pi_s^A(\pi_m)) = \frac{d}{d\pi}u^A(\pi_s^A(\pi_m)) \geq \frac{d}{d\pi}U_r(\pi_s^A(\pi_m)),$$

by the definition of D . And if $\pi_s^A(\pi_m) < \pi_L$, this contradicts (A6). ■

Proof of Proposition 2. The proof closely follows its counterpart for Proposition 1. Part (i) directly follows from part (i) of Lemma 9.

Next consider part (iv). This claim directly follows from parts (ii) and (iii) of Lemma 9 where we relabel π_l (i.e., the lowest value of π for which $(\pi, U(\pi))$ is supported by $a = \mathcal{A}$) as π^A .

Finally, consider parts (ii) and (iii). We know that $(\pi^O, U(\pi^O))$ is supported by $a = R$. For any $\pi \in (\pi^O, \pi^A)$ consider the payoff pair $(\pi, U(\pi))$. Note that $(\pi, U(\pi))$ cannot be supported by $a = A$ since $u^A(\pi) > u^A(\pi)$ for all $\pi \geq (1-\delta)y$, and $a = A$ is not feasible when $\pi < (1-\delta)y$. Moreover, it also cannot be supported by $a = O$ or $a = \mathcal{O}$ as these actions can support payoffs on the frontier only if $\pi < \delta\pi^O$ (by Lemma 9, part (i)). Hence, $(\pi, U(\pi))$ must be supported either by $a = R$ or by randomization. Let π^R be the highest value of π such that $(\pi, U(\pi))$ is supported by $a = R$ (again, π^R exists as both U and u_r^R are continuous). So, $U(\pi^R) = u_r^R(\pi^R)$. Moreover, as $U(\pi^R) \geq U_r(\pi^R) \geq u_r^R(\pi^R)$, we have $U(\pi^R) = u_r^R(\pi^R) = U_r(\pi^R)$. But this implies $U(\pi) = U_r(\pi)$ for all $\pi \in [\pi^O, \pi^R]$ as $U'(\pi) \geq U_r'(\pi)$ for all $\pi < \pi^A$ (by (A6)). Now, since $U_r(\pi^R) = u_r^R(\pi^R)$, i.e. $(\pi^R, U_r(\pi^R))$ is sustained by the rigid action, it follows directly from the characterization of U_r that $U_r(\pi) = u_r^R(\pi)$ for all $\pi \in [\pi^O, \pi^R]$. Hence, $U(\pi) = U_r(\pi) = u_r^R(\pi)$ for all $\pi \in [\pi^O, \pi^R]$.

Finally, if $\pi^R < \pi^A$, by definition of π^R and the argument given above, it directly follows that for any $\pi \in (\pi^R, \pi^A)$, $(\pi, U(\pi))$ must be sustained by randomization between two PPE payoffs, one sustained by R and the other by \mathcal{A} . Hence, $U(\pi)$ must be linear if $\pi \in (\pi^R, \pi^A)$,

and without loss of generality, we can assume that the two end points are $(\pi^R, U(\pi^R))$ and $(\pi^A, U(\pi^A))$. ■

Proof of Lemma 5. We have already shown $\pi^O = \pi_r^O = (1 - \delta)py$ and $\bar{\pi} > \bar{\pi}_r$ in Lemma 9.

To see why $\pi^R \leq \pi_r^R$, suppose on the contrary, $\pi^R > \pi_r^R$. Since $(\pi^R, U(\pi^R))$ is sustained by $a = R$, $U(\pi^R) = u_r^R(\pi^R)$. But $\pi^R > \pi_r^R$ implies $U_r(\pi^R) > u_r^R(\pi^R)$, and hence, we must have $U_r(\pi^R) > U(\pi^R)$, which is a contradiction (as $U_r(\pi) \leq U(\pi)$ for all π).

That $U_r(\pi) = U(\pi)$ for all $\pi \leq \pi^R$ follows from Proposition 1 and 2. Next, we show that $U(\pi) > U_r(\pi)$ for $\pi > \pi^R$.

Take some $\pi' > \pi^R$. The agent's payoff $U_r(\pi')$ can be supported by either the rigid action, or the adaptive action, or by randomization. If it is supported by the rigid action, $U_r(\pi') = u^R(\pi') < U(\pi')$, where the last inequality follows from the definition of π^R . If $(\pi', U_r(\pi'))$ is supported by the adaptive action $a = A$, then $U_r(\pi') = u^A(\pi') < u^A(\pi') \leq U(\pi')$, where the first inequality has been proved above in Step 1 of the proof of Lemma 9, and the second one follows from the definition of U . Finally, if $(\pi', U_r(\pi'))$ is supported by randomization, it must be that $\pi' \in (\pi_r^R, \pi_r^A)$, and there exists a $\lambda \in (0, 1)$ such that $U_r(\pi') = \lambda U_r(\pi_r^A) + (1 - \lambda) U_r(\pi_r^R)$. Since $(\pi_r^A, U(\pi_r^A))$ is supported by $a = A$, we have $U(\pi_r^A) > U_r(\pi_r^A)$ (as argued above). But this implies that

$$U(\pi') \geq \lambda U(\pi_r^A) + (1 - \lambda) U_r(\pi_r^R) > \lambda U_r(\pi_r^A) + (1 - \lambda) U_r(\pi_r^R) = U_r(\pi'),$$

where the first inequality follows from the fact that both $(\pi_r^A, U(\pi_r^A))$ and $(\pi_r^R, U_r(\pi_r^R))$ are in \mathcal{E} . ■

Proof of Proposition 4. Part (i). First consider the case where the standardized procedure is already in place. Recall that in this case the PPE payoff set is \mathcal{E}_r and the PPE payoff frontier is U_r .

Step 1A. Let $\hat{\pi} := (1 - \delta)y$. This is the lowest value of π for which the adaptive action is feasible. The proof consists of showing that for some parameters

$$(A9) \quad U_r(\pi_r^O) + (\hat{\pi} - \pi_r^O) \frac{d}{d\pi} u_r^A(\hat{\pi}) > u_r^A(\hat{\pi}),$$

where the derivative can be thought of as the right or left derivative when the derivative fails to exist. (We also maintain this convention with the notation in the remainder of

the proof.) Recall that $\pi_r^O = (1 - \delta)py$. If this condition is satisfied, then the slope of $u_r^A(\pi)$ evaluated at $\pi = \hat{\pi}$ is greater than the slope of the line that connects the points $(\pi_r^O, U_r(\pi_r^O))$ and $(\hat{\pi}, u_r^A(\hat{\pi}))$, which implies that there exists $\pi' > \hat{\pi}$ and $\lambda \in (0, 1)$ such that $(1 - \lambda)\pi_r^O + \lambda\pi' = \hat{\pi}$ and $(1 - \lambda)U_r(\pi_r^O) + \lambda u_r^A(\pi') > u_r^A(\hat{\pi})$. In other words, there is a randomization between the points $(\pi_r^O, U_r(\pi_r^O))$ and $(\pi', u_r^A(\pi'))$ that for $\pi = \hat{\pi}$ yields a payoff to the agent strictly greater than $u_r^A(\hat{\pi})$. But this implies that $U_r(\hat{\pi}) > u_r^A(\hat{\pi})$, which means that the point $(\hat{\pi}, U_r(\hat{\pi}))$ on the payoff frontier requires playing the rigid action in the current period with a positive probability. That is, the firm may ask the worker to perform the rigid action even though the adaptive action is feasible.

Step 1B. We next show that there are parameter values for which (A9) is satisfied. Recall from (A8) that

$$\frac{d}{d\pi} u_r^A(\pi) = \theta \frac{d}{d\pi} U_r(\pi_s^A(\pi)) - (1 - \theta).$$

Since $\pi_s^A(\hat{\pi}) = 0$,

$$\frac{d}{d\pi} u_r^A(\hat{\pi}) = \theta \frac{d}{d\pi} U_r(0) - (1 - \theta) = \theta \frac{U_r(\pi_r^O)}{(1 - \delta)py} - (1 - \theta).$$

(Recall that U_r is linear for $\pi < \pi_r^O$ and its slope is given by $U_r(\pi_r^O)/((1 - \delta)py)$). Given this and that $\hat{\pi} - \pi_r^O = (1 - \delta)(1 - p)y$, we can write (A9) as

$$(A10) \quad U_r(\pi_r^O) + \left(\theta \frac{U_r(\pi_r^O)}{(1 - \delta)py} - (1 - \theta) \right) (1 - \delta)(1 - p)y > u_r^A(\hat{\pi}).$$

Step 1C. Now, since $(\pi_r^O, U_r(\pi_r^O))$ is sustained by the rigid action, by adding (PK_A^R) and (PK_P^R) and re-arranging we obtain that

$$(A11) \quad U_r(\pi_r^O) = -(1 - \delta)c + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)).$$

Similarly, we can write

$$u_r^A(\hat{\pi}) = -(1 - \delta)C + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)).$$

Hence, $u_r^A(\hat{\pi}) = U_r(\pi_r^O) - (1 - \delta)(C - c)$, and we can write (A10) as

$$\left(\theta \frac{U_r(\pi_r^O)}{(1 - \delta)py} - (1 - \theta) \right) (1 - \delta)(1 - p)y > -(1 - \delta)(C - c).$$

Rearranging terms, we obtain that this inequality is equivalent to

$$(A12) \quad (\theta U_r(\pi_r^O) - (1 - \theta)(1 - \delta)py) \frac{1 - p}{p} > -(1 - \delta)(C - c).$$

Step 1D. Now, from (A11) and the fact that $\bar{\pi}_r + U_r(\bar{\pi}_r) \geq (1 - \delta)(y - C)/(1 - (1 - \theta)\delta)$ (see Step R3 of the proof of Lemma 7) we obtain that

$$U_r(\pi_r^O) \geq -(1 - \delta)c + (1 - \theta)\delta \frac{(1 - \delta)(y - C)}{1 - (1 - \theta)\delta}.$$

Thus, a sufficient condition for (A9) is that

$$(A13) \quad \theta \left(c - (1 - \theta)\delta \frac{y - C}{1 - (1 - \theta)\delta} \right) + (1 - \theta)py < \frac{p(C - c)}{1 - p}.$$

There are parameters values that satisfy this condition as well as all the other assumptions of the model. For example, if $\theta\delta(1 - p) - p(1 - \delta) > 0$ (a condition compatible with Assumption 1 (ii)), the left-hand side of the above inequality increases with y and is satisfied when y sufficiently large.

Now consider the case where the standardized procedure has not been in place. In this case the PPE payoff set is \mathcal{E} and the PPE payoff frontier is U . The proof is analogous to that above.

Step 2A. We need to show that there are parameter values for which

$$(A14) \quad U(\pi^O) + (\hat{\pi} - \pi^O) \frac{d}{d\pi} u^A(\hat{\pi}) > u^A(\hat{\pi}).$$

Recall that $\pi^O = \pi_r^O$ and that $U(\pi^O) = U_r(\pi_r^O)$. Hence, the only difference relative to the proof above is that we have $\frac{d}{d\pi} u^A(\hat{\pi})$ instead of $\frac{d}{d\pi} u_r^A(\hat{\pi})$ and $u^A(\hat{\pi})$ instead of $u_r^A(\hat{\pi})$.

We first show that $\frac{d}{d\pi} u^A(\hat{\pi}) = \frac{d}{d\pi} u_r^A(\hat{\pi})$. Recall that

$$\frac{d}{d\pi} u^A(\pi) = \theta \frac{d}{d\pi} U(\pi_s^A(\pi)) - (1 - \theta).$$

Since $\pi_s^A(\hat{\pi}) = 0$,

$$\frac{d}{d\pi} u^A(\hat{\pi}) = \theta \frac{d}{d\pi} U(0) - (1 - \theta) = \theta \frac{U(\pi^O)}{(1 - \delta)py} - (1 - \theta) = \theta \frac{U_r(\pi_r^O)}{(1 - \delta)py} - (1 - \theta),$$

where the second equality follows from the fact that $U(\pi) = U_r(\pi)$ for $\pi \leq \pi^O$ and $\pi^O = \pi_r^O$. Thus, $\frac{d}{d\pi} u^A(\hat{\pi}) = \frac{d}{d\pi} u_r^A(\hat{\pi})$.

Step 2B. We now analyze $u^A(\hat{\pi})$ and $U(\pi^O)$. As mentioned above,

$$U(\pi^O) = U_r(\pi_r^O) = -(1 - \delta)c + (1 - \theta)\delta(\bar{\pi}_r + U_r(\bar{\pi}_r)).$$

Similarly, we have that

$$u^A(\hat{\pi}) = -(1 - \delta)C + (1 - \theta)\delta(\bar{\pi} + U(\bar{\pi})).$$

Thus,

$$\begin{aligned}
 (A15) \quad u^A(\widehat{\pi}) - U(\pi^O) &= -(1 - \delta)(C - c) + (1 - \theta)\delta[\bar{\pi} + U(\bar{\pi}) - (\bar{\pi}_r + U_r(\bar{\pi}_r))] \\
 &\leq -(1 - \delta)(C - c) + (1 - \theta)\delta\left((y - C) - \frac{(1 - \delta)(y - C)}{1 - (1 - \theta)\delta}\right) \\
 &= -(1 - \delta)(C - c) + \delta^2 \frac{\theta(1 - \theta)(y - C)}{1 - (1 - \theta)\delta},
 \end{aligned}$$

where the inequality follows from the fact that $\bar{\pi} + U(\bar{\pi}) \leq y - C$ (recall that $y - C$ is the maximum surplus possible) and that $\bar{\pi}_r + U_r(\bar{\pi}_r) \geq (1 - \delta)(y - C)/(1 - (1 - \theta)\delta)$ (from Step R3 of the proof of Lemma 7).

Step 2C. Now, rearrange the condition (A14) as follows:

$$(\widehat{\pi} - \pi^O) \frac{d}{d\pi} u^A(\widehat{\pi}) > u^A(\widehat{\pi}) - U(\pi^O).$$

A lower bound for the left-hand side of this inequality is given by the left-hand side of the inequality (A13). And from (A15) we obtain an upper bound for the right-hand side. Plugging these bounds we obtain a sufficient condition for (A14) as:

$$(A16) \quad \theta \left(c - (1 - \theta)\delta \frac{(1 - p - \delta)(y - C)}{(1 - \delta)(1 - p)(1 - (1 - \theta)\delta)} \right) + (1 - \theta)py < \frac{p(C - c)}{1 - p}.$$

There are parameter values for which this condition is satisfied along all the other assumptions of the model. In particular, if

$$\theta\delta(1 - p - \delta) > p(1 - p)(1 - \delta)(1 - (1 - \theta)\delta),$$

then the left-hand side of the condition is increasing in y and for sufficient high values of y it is satisfied. Also note that whenever (A16) is satisfied, so is (A13). So, the precautionary use of the rigid action is more likely to occur when the standard work process has already been put in place.

Part (ii). **Step 1.** Define $T_1(\pi) = \pi_s^A(\pi)$, $T_2(\pi) = \pi_s^A(\pi_s^A(\pi))$, and $T_n(\pi)$ is defined accordingly. Also, let N be the number of consecutive shocks that guarantees that the rigid action is used when the relationship starts in Phase 1 (i.e., when the standardized procedure is yet to be established and the relationship starts with payoffs $(\bar{\pi}, 0)$). Similarly, let N_r be its counterpart when the relationship starts in Phase 2 (i.e., when the standardized procedure has been established and the relationship starts with payoffs $(\bar{\pi}_r, u^*)$). Recall that $\pi_s^A(\pi) = \pi_s^A(\pi)$. Hence, $N = \min\{n \mid T_n(\bar{\pi}) \leq \pi^R\}$ and $N_r = \min\{n \mid T_n(\bar{\pi}_r) \leq \pi_r^R\}$.

Step 2. Also note that $\pi_s^A(\pi^A) \leq \pi^R$, as otherwise one can move both π_s^A and π_n^A to the left by $\varepsilon > 0$ and increase the payoff of the agent. (That is, when the relationship starts in Phase 1 and a series of consecutive shocks calls for randomization between $a = \mathcal{A}$ and $a = R$

for the very first time, even if $a = \mathcal{A}$ is realized in the current period, another shock in the current period surely move the relationship to Phase 2.) So, as $\pi^R \leq \pi_r^R$ and $\bar{\pi} > \bar{\pi}_r$, we have $N \geq N_r$. (Also note that even if $N = N_r$, the principal's payoff when the rigid action is used is lower if started out from $\bar{\pi}_r$ than if we start from $\bar{\pi}$. That is, at π^A the continuation payoff of the agent following a shock π_s^A is weakly smaller than π^R . If not, then one can move both π_s^A and π_n^A to the left by $\varepsilon > 0$ and increase the payoff of the agent.) ■

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