

Managing Conflicts in Relational Contracts[†]

By JIN LI AND NIKO MATOUSCHEK*

A manager and a worker are in an infinitely repeated relationship in which the manager privately observes her opportunity costs of paying the worker. We show that the optimal relational contract generates periodic conflicts during which effort and expected profits decline gradually but recover instantaneously. To manage a conflict, the manager uses a combination of informal promises and formal commitments that evolves with the duration of the conflict. Finally, we show that liquidity constraints limit the manager's ability to manage conflicts but may also induce the worker to respond to a conflict by providing more effort rather than less. (JEL C73, D74, D86, J33, J41, M12)

Relational contracts often suffer from conflicts during which workers punish managers for broken promises. A common cause for such conflicts is disagreement over the availability and efficient use of funds. In a typical conflict of this sort, workers demand that a bonus be paid while managers insist that the necessary funds are either nonexistent or would be better spent on something else, such as an exceptional investment opportunity.

One source of disagreement over the availability and efficient use of funds is asymmetric information. Managers are typically better informed about the challenges and opportunities that their firms face and therefore often have private information about the opportunity costs of paying their workers. The aim of this article is to explore optimal relational contracts in such a setting. For this purpose, we examine the repeated relationship between a manager and a worker in which the manager's opportunity costs of paying the worker are stochastic and privately observed by her. In the optimal relational contract, the manager promises a bonus if opportunity costs are low but none if they are high. Conflicts therefore arise whenever the manager does not pay the bonus. To manage these conflicts, the manager relies on a combination of informal promises and formal commitments that evolves with the duration of the conflict. As a result, effort and expected profits decline during a conflict only gradually and then recover instantaneously. The same pattern is repeated over time.

*Li: Department of Management and Strategy, Kellogg School of Management, Northwestern University, 2001 Sheridan Road, Evanston, IL 60208 (e-mail: jin-li@kellogg.northwestern.edu); Matouschek: Department of Management and Strategy, Kellogg School of Management, Northwestern University, 2001 Sheridan Road, Evanston, IL 60208 (e-mail: n-matouschek@kellogg.northwestern.edu). We have no financial or other material interests related to this research to disclose. We thank three anonymous referees, Maja Butovich, Anne Duchene, Florian Ederer, Matthias Fahn, Yuk-Fai Fong, Bob Gibbons, Marina Halac, Tom Hubbard, Ed Lazear, Arijit Mukherjee, Mike Powell, Michael Raith, Takuro Yamashita, Pierre Yared, and the participants at various seminars and conferences for their comments and suggestions. All remaining errors are, of course, our own.

[†] Go to <http://dx.doi.org/10.1257/aer.103.6.2328> to visit the article page for additional materials and author disclosure statement(s).

The relationship between the manager and the worker therefore never terminates, nor does it reach a steady state. Instead, it cycles indefinitely.

The Lincoln Electric Company provides an example of the type of situation that motivates this article. In the early 1990s, Lincoln Electric was a leading manufacturer of welding machines, well known for its promise to share a significant fraction of profits with its factory workers. In 1992, Lincoln's US business had generated a significant profit and, as a result, its US workers expected to be paid their bonus. Mounting losses in its recently acquired foreign operations, however, more than wiped out US profits. This presented CEO Donald Hastings with a dilemma: "Our 3,000 US workers would expect to receive, as a group, more than \$50 million. If we were in default, we might not be able to pay them. But if we didn't pay the bonus, the whole company might unravel" (Hastings 1999, p. 164). To prevent the company from unraveling, Hastings decided to borrow \$52.1 million and pay the bonus.

Why would Hastings have to take the seemingly inefficient step of borrowing money to pay the bonus? After all, the bonus was explicitly a "cash-sharing bonus" and US workers had a long history of accepting fluctuations in the bonus in response to fluctuations in US profits. The reason, it seems, was that US workers were unable to observe foreign losses and therefore did not know whether US profits really were needed to cover those losses. This explains why shortly after he paid the bonus, Hastings "instituted a financial education program so that employees would understand that no money was being hidden from them" (Hastings 1999, p. 172).

The Lincoln Electric case illustrates the issues that arise if a manager is privately informed about the opportunity costs of paying her worker. In such a setting, if the manager does not pay a bonus, the worker cannot observe her motives. Is the manager not paying the bonus because it is more efficient to spend resources on something else, as she claims? Or is she just making up an excuse to extract some of the worker's rents? To keep the manager honest, the worker must then punish her whenever she does not pay a bonus. As a result, the manager faces a trade-off between the current benefits of adapting bonus payments to their opportunity costs and the future costs the worker inflicts on her if she does not pay a bonus. In short, the manager faces a trade-off between the benefits of adaptation and the costs of conflict.

To explore this trade-off, we examine a firm that consists of a risk-neutral owner-manager and a risk-neutral but liquidity-constrained worker. Output and effort are observable but not contractible. At the beginning of every period the manager offers the worker a contractible wage and a noncontractible bonus. After accepting the offer, the worker decides on his effort level. Effort is continuous and imposes a cost on the worker. Finally, output is realized, and the manager decides how much to pay the worker. So far this is a relational contracting model with public information that is well understood (MacLeod and Malcomson 1989). The only change we make to this standard model is to assume that the manager's opportunity costs of paying the worker are stochastic and privately observed by her. In particular, just before the manager decides how much to pay the worker, she observes whether the firm has been hit by a shock—in which case opportunity costs are high—or not—in which case they are low.

In this setting, it is optimal for the manager to motivate the worker by promising to pay him a bonus. The bonus, however, is contingent on opportunity costs being low. To keep the manager honest, the worker punishes her when she does not pay

a bonus and rewards her when she does. In particular, if the manager does not pay the bonus this period, expected profits will be lower next period, unless they are already at their lower bound, in which case they stay there. In contrast, expected profits immediately jump to their upper bound if the manager does pay the bonus. Expected profits therefore cycle indefinitely, and the relationship never terminates. These cycles differ in length depending on the number of consecutive shock periods the firm experiences. They all, however, follow the same pattern in which downturns are gradual and recoveries instantaneous. In our setting, it is therefore not optimal for the parties to alternate between high profit “cooperation” phases and low profit “punishment” phases, as in Green and Porter (1984). Nor is it optimal for them to adopt termination contracts in which the failure to pay the bonus triggers the termination of their relationship with some probability, as in Levin (2003).

One reason for why downturns are gradual and recoveries instantaneous is that joint surplus is increasing in expected profits. Essentially, the larger is the manager’s stake in the relationship, the less tempted she is to renege, and thus the more effort the worker is willing to provide. Rewarding the manager for paying a bonus is therefore not only good for her incentives to act truthfully but is also efficiency enhancing. As a result, it is optimal for expected profits to jump to their upper bound when the manager pays the bonus. In contrast, punishing the manager for not paying the bonus destroys joint surplus. Since the production function is concave, the most efficient way to punish the manager is then to reduce profits gradually.

To see how the optimal punishment is implemented, consider a period in which expected profits are not at their lower bound and suppose the manager does not pay the bonus. In the next period, the manager will then have to offer the worker a larger bonus. Moreover, the manager will either have to accept a reduction in effort or offer a higher wage. In particular, the optimal punishment calls for a reduction in effort if expected profits are high and an increase in the wage if they are low. The reason for this pattern is again the concavity of the production function, which makes it more efficient to punish the manager through a reduction in effort if expected profits are high and through an increase in wages if they are low.

The optimal punishment gives rise to conflicts that go through up to three distinct phases. Initially, the manager responds to a conflict by offering the worker a larger and larger bonus, but she does not commit to a wage. In response, the worker provides less and less effort. Once expected profits are sufficiently low, the conflict enters its second phase, during which the manager complements his promise to pay larger and larger bonuses with the formal commitment to also pay higher and higher wages. In response, the worker no longer reduces effort. Finally, expected profits reach their lower bound, and the conflict enters its final phase. During this phase the bonus and the wage stay constant at their maximized levels, and the worker continues to provide the same level of effort. The final phase of the conflict continues until a period in which the firm is not hit by a shock, at which point the conflict ends, and expected profits return to their upper bound.

A key assumption in our model is that the firm is not liquidity constrained. The manager can therefore always pay the worker any positive amount, even if the opportunity costs of doing so may be high. In our main extension we relax this assumption. We show that liquidity constraints limit the manager’s ability to manage conflicts, which slows down recoveries and may lead to termination. They can also,

however, induce the worker to respond to a conflict by providing more effort rather than less. Essentially, the worker understands that more effort relaxes the firm's liquidity constraint, which, in turn, allows the manager to pay him a larger bonus.

To illustrate the role of liquidity constraints in managing relational contracts, we return to the Lincoln Electric case. In early 1993, a few months after he had borrowed the necessary funds to pay his workers, CEO Hastings realized that European losses would once again wipe out US profits. The covenants in the debt that he took on the previous year, however, prevented him from again borrowing the necessary funds to pay the bonus:

... we turned to our US employees for help. I presented a 21-point plan to the board that called for our US factories to boost production dramatically [...]. "We blew it," I said [to the US employees]. "Now we need you to bail the company out. If we violate the covenants, banks won't lend us money. And if they don't lend us money, there will be no bonus in December." (Hastings 1999, pp. 171–72)

According to Hastings, his "statement appealed not only to [the US workers'] loyalty but also to what James F. Lincoln called their 'intelligent selfishness'" (Hastings 1999, p. 172). And, apparently, it worked: "Thanks to the Herculean effort in the factories and in the field, we were able to increase revenues and profits enough in the United States to avoid violating our loan covenants" (Hastings 1999, p. 178).

As a result, Hastings was able to renew the covenants, which, in turn, allowed him to once again borrow the necessary funds and pay the bonus. In line with the reasoning that we sketched above, therefore, Lincoln Electric's US workers increased their efforts so as to relax the firm's liquidity constraints, which, in turn, ensured that they were paid their bonus.

I. Related Literature

There is a large literature that examines relational contracts both between and within firms; see MacLeod (2007) and Malcomson (2013) for recent reviews. Our article contributes to the branch of this literature that studies the actions managers can take to sustain relational contracts better, such as the timing of payments (MacLeod and Malcomson 1998), the design of explicit contracts (Baker, Gibbons, and Murphy 1994; Che and Yoo 2001), the allocation of ownership rights (Baker, Gibbons, and Murphy 2002; Rayo 2007), the differential treatment of workers (Levin 2002), the grouping of tasks (Mukherjee and Vasconcelos 2011), and others. In contrast to these papers, our focus is on how to manage conflicts once they arise, rather than on how to prevent them in the first place.

Our article contributes to the branch of the literature on relational contracts in which the manager is privately informed about aspects of the relationship. In this context, three closely related papers are Levin (2003), Fuchs (2007), and Englmaier and Segal (2011). In the second part of Levin (2003), the manager privately observes the worker's performance. In contrast to our setting, the worker's effort is privately observed, which makes joint punishments necessary. Levin shows that the optimal contract is stationary and can be implemented through a termination contract. In the same setting, Fuchs (2007) allows for private monitoring and shows that while the optimal contract can still be

implemented through a termination contract, it is no longer stationary. In both models efficient transfers are always available. In contrast, in our setting efficient transfers are not always available, and as a result termination contracts are not optimal.

Englmaier and Segal (2011) correspond to a version of our model in which effort is binary and the manager's opportunity costs in a shock period are infinite. They focus on a particular relational contract in which the parties alternate between phases with high and low effort. In contrast, we characterize the optimal relational contract and show that under such a contract conflicts evolve more gradually.

Another closely related paper, albeit in a different context, is Yared (2010). He characterizes the optimal sequential equilibria in a game between an aggressive country that demands transfers from a peaceful one, where the peaceful country is privately informed about the costs of paying the transfers. In this setting, the aggressive country can punish the peaceful one through the binary choice of going to war or not. In contrast, in our setting the worker can punish the manager by providing less effort or demanding higher wages, both of which are continuous choices. As a result, optimal temporary conflicts are more gradual in our setting than optimal temporary wars in Yared's paper. Moreover, while in his setting the parties eventually engage in permanent war, termination is never optimal in ours.

Our article also contributes to the recent and growing literature on dynamics within relational contracts. Chassang (2010) studies a model of exploration with private information and shows that the relationship is path dependent and can settle in different long-run equilibria. Fong and Li (2010) study a moral hazard problem in which the worker has limited liability and explore patterns of the worker's job security, pay level, and the sensitivity of pay to performance. Padro i Miquel and Yared (2012) examine a political economy model and study the likelihood, duration, and intensity of war. Thomas and Worrall (2010) examine a partnership game with perfect information and two-sided limited liability. They show that the relationship becomes more efficient over time as the division of future rents becomes more equal. Dynamics also arise in models of relational contracts in which agents have private and fixed types; see, for example, Halac (2012), Watson (1999, 2002), and Yang (2013). In these papers, dynamics arise when the principal updates her beliefs about the agent's type.

In terms of its analytical structure, our model is related to the literature on dynamic games with hidden information; see, for example, Abdulkadiroğlu and Bagwell (2013), Athey and Bagwell (2001, 2008), Athey, Bagwell, and Sanchirico (2004), Hauser and Hopenhayn (2008), Möbius (2001), and for surveys, Mailath and Samuelson (2006) and Samuelson (2006). A distinct feature of our model is the occasional availability of efficient transfers. As a result, the dynamics in our model feature gradual downturns or instantaneous recoveries.

Our model is also related to the literature on dynamic contracting between banks and privately informed entrepreneurs (DeMarzo and Fishman 2007; DeMarzo and Sannikov 2006; Biais et al. 2007; and Clementi and Hopenhayn 2006). In contrast to this literature, we focus on a setting in which long-term contracts are not feasible. The unavailability of long-term contracts is crucial for our results. In particular, we show in Section VI that if the long-term contracts were feasible, the parties could approximate first-best.

Finally, since the efficiency of transfers depends on the state of the world, our model is related to the large literature on risk sharing. Kocherlakota (1996) and

Ligon, Thomas, and Worrall (2002) explore efficient risk sharing between risk-averse agents when information is public and commitment is limited. Hertel (2004) examines the case with two-sided asymmetric information without commitment. Thomas and Worrall (1990) study a one-sided asymmetric information problem with commitment. This literature typically assumes that the players' endowments are exogenously given and path independent. In our model, instead, output depends on the worker's effort and, thus, on how it was divided in the past.

II. The Model

A firm consists of a risk-neutral owner-manager and a risk-neutral but liquidity-constrained worker. The manager and the worker are in an infinitely repeated relationship. Time is discrete and denoted by $t = \{1, 2, \dots, \infty\}$.

At the beginning of any period t the manager makes the worker an offer. The offer consists of a contractible commitment to pay wage $w_t \geq 0$ and a noncontractible promise to pay bonuses $b_{s,t}$ and $b_{n,t}$, where s and n stand for "shock" and "no-shock." The worker either accepts the offer or rejects it. We denote the worker's decision by d_t , where $d_t = 0$ if he rejects the offer and $d_t = 1$ if he accepts it. If the worker rejects the offer, the manager and the worker realize their per-period outside options $\underline{\pi} > 0$ and $\underline{u} > 0$, and time moves on to period $t + 1$.

If, instead, the worker accepts the manager's offer, he next decides on his effort level $e_t \geq 0$. Effort is costly to the worker, and we denote his effort costs by $c(e_t)$. The cost function is strictly increasing and strictly convex with $c(0) = c'(0) = 0$ and $\lim_{e \rightarrow \infty} c'(e) = \infty$. After the worker provides effort e_t , the manager realizes output $y(e_t)$. The output function is strictly increasing and strictly concave with $y(0) = 0$. Effort e_t , effort costs $c(e_t)$, and output $y(e_t)$ are observable but not contractible.

After the manager realizes output $y(e_t)$, she privately observes the state of the world $\Theta_t \in \{s, n\}$, where, as mentioned above, s and n stand for "shock" and "no-shock." The states are drawn independently across time from a binary distribution. The probability with which a shock state occurs is given by $\theta \in (0, 1)$. The state of the world determines the opportunity cost of paying the worker: if the firm is not hit by a shock, paying the worker an amount of $w + b$ costs the manager $w + b$; if, instead, the firm is hit by a shock, paying the worker $w + b$ costs the manager $(1 + \alpha)(w + b)$, where $\alpha \in (0, \infty)$. We do not model explicitly why opportunity costs may be high. As discussed above, however, managers do sometimes face high opportunity costs of paying their workers. This may be the case, for instance, because they need to borrow money to make their payments, as in the Lincoln Electric case.

After the manager observes the state of the world, she pays the worker the wage w_t and a bonus $b_t \geq 0$. Since the promised bonus is not contractible, the payment b_t can be different from the promises $b_{n,t}$ and $b_{s,t}$.

Finally, at the end of period t , the manager and the worker observe the realization x_t of a public randomization device. This allows the players to publicly randomize at the beginning of any period $t + 1 \geq 2$ based on the realization of the public randomization device observed at the end of the previous period. To allow the players to publicly randomize in period one, we assume that they can also observe a realization of the randomization device at the beginning of that period. We denote this realization by x_0 . The existence of a public randomization device is a common assumption

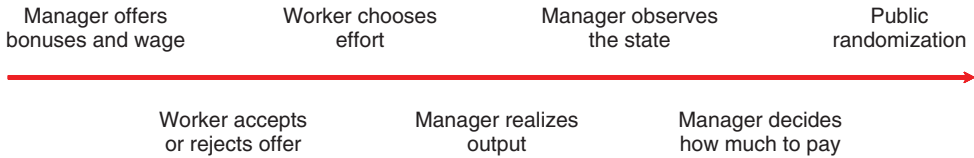


FIGURE 1. TIMELINE

in the literature and is made to convexify the set of equilibrium payoffs. The timing is summarized in Figure 1.

The manager and the worker share the same discount factor $\delta \in (0, 1)$. At the beginning of any period t , their respective expected payoffs are therefore given by

$$\pi_t = (1 - \delta) \sum_{\tau=t}^{\infty} \delta^{\tau-t} \mathbb{E}[d_{\tau}[y(e_{\tau}) - (1 + 1_{\{\theta_t=s\}}\alpha)(w_{\tau} + b_{\tau})] + (1 - d_{\tau})\underline{\pi}]$$

and

$$u_t = (1 - \delta) \sum_{\tau=t}^{\infty} \delta^{\tau-t} \mathbb{E}[d_{\tau}(w_{\tau} + b_{\tau} - c(e_{\tau})) + (1 - d_{\tau})\underline{u}].$$

Note that we multiply the right-hand side of each expression by $(1 - \delta)$ to express profits and payoffs as per-period averages.

We follow the literature on imperfect public monitoring and define a “relational contract” as a pure-strategy Perfect Public Equilibrium (henceforth PPE) in which the manager and the worker play public strategies and, following every history, the strategies are a Nash Equilibrium. Public strategies are strategies in which the players condition their actions only on publicly available information. In particular, the manager’s strategy does not depend on her past private information. Our restriction to pure strategy is without loss of generality because our game has only one-sided private information and is therefore a game with the product structure (see, for instance, p. 310 in Mailath and Samuelson 2006). In this case, there is no need to consider private strategies since every sequential equilibrium outcome is also a PPE outcome (see, for instance, p. 330 in Mailath and Samuelson 2006).

Formally, let $h_{t+1} = \{w_{\tau}, b_{n,\tau}, b_{s,\tau}, d_{\tau}, e_{\tau}, b_{\tau}, x_{\tau}\}_{\tau=1}^t$ denote the public history at the beginning of any period $t + 1$ and let \mathcal{H}_{t+1} denote the set of period $t + 1$ public histories. Note that $\mathcal{H}_1 = \Phi$. A public strategy for the manager is a sequence of functions $\{W_t, B_{s,t}, B_{n,t}, B_t\}_{t=1}^{\infty}$, where $W_t: \mathcal{H}_t \rightarrow [0, \infty)$, $B_{s,t}: \mathcal{H}_t \rightarrow [0, \infty)$, $B_{n,t}: \mathcal{H}_t \rightarrow [0, \infty)$, and $B_t: \mathcal{H}_t \cup \{w_t, b_{s,t}, b_{n,t}, d_t, e_t, \theta_t\} \rightarrow [0, \infty)$. Similarly, a public strategy for the worker is a sequence of functions $\{D_t, E_t\}_{t=1}^{\infty}$, where $D_t: \mathcal{H}_t \cup \{w_t, b_{s,t}, b_{n,t}\} \rightarrow \{0, 1\}$ and $E_t: \mathcal{H}_t \cup \{w_t, b_{s,t}, b_{n,t}, d_t\} \rightarrow [0, \infty)$.

We define an “optimal relational contract” as a PPE with payoffs that are not Pareto-dominated by any other PPE. Note that when the discount factor is sufficiently small, the only relational contract is a trivial one in which the parties always take their outside options $\underline{\pi}$ and \underline{u} . To make the analysis interesting, we assume that the parties are sufficiently patient so that a nontrivial relational contract exists. A sufficient condition for a nontrivial relational contract to exist is

$$y(e^{FB}) - \underline{\pi} - (1 + \alpha\theta)(c(e^{FB}) + \underline{u}) \geq \frac{1 - \delta}{\delta} (1 + \alpha\theta)c(e^{FB}),$$

where e^{FB} is the first-best effort that maximizes $y(e) - c(e)$.

III. Preliminaries

In this section we first list the constraints that have to be satisfied for a payoff pair to be in the PPE payoff set. We then consider a relaxed problem that ignores one of these constraints. For this relaxed problem we characterize properties of the PPE payoff set in Section IIIB and properties of the optimal relational contract in Section IIIC. These properties of the relaxed problem will then allow us to characterize the optimal relational contract in Section IV.

A. The Constraints

We denote the set of PPE payoffs by \mathcal{E} . Each payoff pair $(\pi, u) \in \mathcal{E}$ is associated with a profile of actions (e, w, b_s, b_n) and continuation payoffs (π_s, π_n, u_s, u_n) , where π_s and π_n are the manager's continuation payoffs associated with shock and no-shock states, and u_s and u_n are defined analogously. We say that a PPE payoff pair (π, u) can be "supported" by pure actions if there exists a profile of actions (e, w, b_s, b_n) and continuation payoffs (π_s, π_n, u_s, u_n) that satisfy the following three sets of constraints.

Feasibility.—For the actions to be feasible, the wage, bonuses, and effort have to be nonnegative. Specifically, the nonnegativity constraints are given by

$$(NN_w) \quad w \geq 0,$$

$$(NN_n) \quad b_n \geq 0,$$

$$(NN_s) \quad b_s \geq 0,$$

and

$$(NN_e) \quad e \geq 0.$$

Moreover, for the continuation payoffs to be feasible, they also need to be PPE payoffs. The self-enforcing constraints are therefore given by

$$(SE_n) \quad (\pi_n, u_n) \in \mathcal{E}$$

in a no-shock period and

$$(SE_s) \quad (\pi_s, u_s) \in \mathcal{E}$$

in a shock period.

No Deviations.—To ensure that neither party deviates, we need to consider both off- and on-schedule deviations. Off-schedule deviations are deviations that can be publicly observed. There is no loss of generality in assuming that if an off-schedule

deviation occurs, the parties terminate their relationship, as this is the worst possible equilibrium that gives each party its minmax payoff.

The manager deviates off-schedule when he pays a bonus that is different from either b_s or b_n . If the manager does deviate off-schedule, she cannot do better than to pay a zero bonus. The nonrenewing constraints are therefore given by

$$(NR_N) \quad \delta\pi_n - \delta\underline{\pi} \geq (1 - \delta)b_n$$

in a no-shock period and

$$(NR_S) \quad \delta\pi_s - \delta\underline{\pi} \geq (1 - \delta)(1 + \alpha)b_s$$

in a shock period.

The worker deviates off-schedule when he rejects the manager's offer or provides an effort level that is different from e . The individual rationality constraint

$$(IR_W) \quad u \geq \underline{u}$$

ensures that the worker does not reject the manager's offer. If the worker accepts the offer but deviates by providing an effort level that is different from e , he cannot do better than to provide no effort. The worker's incentive constraint is therefore given by

$$(IC_W) \quad u \geq (1 - \delta)w + \delta\underline{u}.$$

In contrast to off-schedule deviations, on-schedule deviations are only privately observed. Since the worker does not have any private information, he cannot engage in any on-schedule deviations. The manager, however, can do so by either paying b_n in a shock period or b_s in a no-shock period. The manager's truth-telling constraints are therefore given by

$$(TT_N) \quad \delta(\pi_n - \pi_s) \geq (1 - \delta)(b_n - b_s)$$

in a no-shock period and

$$(TT_S) \quad \delta(\pi_n - \pi_s) \leq (1 + \alpha)(1 - \delta)(b_n - b_s)$$

in a shock period.

Promise Keeping.—Finally, the consistency of the PPE payoff decomposition requires that the parties' payoffs are equal to the weighted sum of current and future payoffs. The promise-keeping constraints are therefore given by

$$(PK_M) \quad \begin{aligned} \pi = & \theta\{(1 - \delta)[y(e) - (1 + \alpha)(w + b_s)] + \delta\pi_s\} \\ & + (1 - \theta)\{(1 - \delta)[y(e) - w - b_n] + \delta\pi_n\} \end{aligned}$$

for the manager and

$$(PK_w) \quad u = \theta[(1 - \delta)(w + b_s) + \delta u_s] \\ + (1 - \theta)[(1 - \delta)(w + b_n) + \delta u_n] - (1 - \delta)c(e)$$

for the worker.

B. Properties of the PPE Payoff Set

Before characterizing the optimal relational contract that satisfies all the constraints in the previous section, we first turn to a relaxed problem that ignores the worker's incentive constraint IC_w . To streamline the exposition, however, we keep the same notation as above.

Specifically, we now use the technique developed by Abreu, Pearce, and Stacchetti (1990) to characterize the PPE payoff set \mathcal{E} of the relaxed problem. For this purpose, we define the payoff frontier as

$$u(\pi) \equiv \sup\{u' : (\pi, u') \in \mathcal{E}\}.$$

Our first lemma establishes several properties of the PPE payoff set \mathcal{E} .

LEMMA 1: *The PPE payoff set \mathcal{E} has the following properties: (i) it is compact, (ii) payoff pair (π, u) belongs to \mathcal{E} if and only if $\pi \in [\underline{\pi}, \bar{\pi}]$ and $u \in [\underline{u}, u(\pi)]$, and (iii) the extremal point $u(\bar{\pi})$ satisfies $u(\bar{\pi}) = \underline{u}$.*

A key implication of this lemma is that the PPE payoff set \mathcal{E} is fully characterized by its frontier $u(\pi)$. To see why, notice that for any $u(\pi)$, the points below it can be sustained by randomizing among $(\underline{\pi}, \underline{u})$, $(\bar{\pi}, \underline{u})$, and $(\pi, u(\pi))$. Since the PPE frontier fully characterizes the PPE payoff set, we now turn to the next lemma, which establishes several of its properties.

LEMMA 2: *The PPE frontier $u(\pi)$ has the following properties: for all $\pi \in [\underline{\pi}, \bar{\pi}]$, (i) payoffs $(\pi, u(\pi))$ can be supported by pure actions in the stage game other than taking the outside options, (ii) u is concave, and (iii) u is differentiable with $-1 < u'(\pi) \leq -1/(1 + \alpha\theta)$.*

The first part of the lemma shows that payoffs on the PPE frontier can be supported by pure actions, that is, they do not require any public randomization. This fact will allow us to represent the PPE frontier recursively below. This property follows from the concavity of the output function $y(e)$. Essentially, any PPE that is supported by randomization between two effort levels can be improved upon by having the worker provide an appropriately chosen intermediate level of effort. The concavity of the PPE frontier follows immediately from the availability of a public randomization device, and its differentiability follows from the continuity of effort. Finally, the bounds on the derivative imply that the PPE frontier is downward

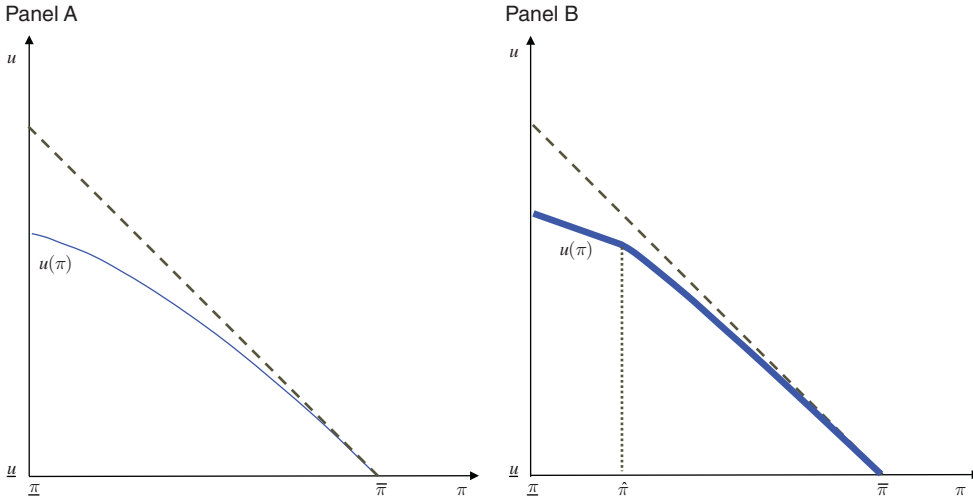


FIGURE 2. THE PPE FRONTIER

sloping and that joint surplus $\pi + u(\pi)$ is increasing in expected profits π and thus maximized at $\bar{\pi}$. Figure 2, panels A and B illustrate these properties.

In both panels the PPE frontier is downward sloping and joint surplus is maximized at $\bar{\pi}$. The difference between the two panels is that in panel A the derivative of the PPE frontier never reaches its upper bound $u'(\pi) = -1/(1 + \alpha\theta)$. In panel B, instead, the derivative does reach this upper bound at a critical level of expected profits $\hat{\pi}$, and as a result the PPE frontier is linear for all $\pi \leq \hat{\pi}$. This critical level of expected profits is defined by

$$(1) \quad \hat{\pi} = (1 - \delta)y(\hat{e}) + \delta\bar{\pi},$$

where \hat{e} is the unique effort level that solves

$$(2) \quad \frac{c'(\hat{e})}{y'(\hat{e})} = \frac{1}{1 + \alpha\theta}.$$

Notice that $\hat{\pi}$ can be smaller than $\bar{\pi}$, as in panel A, or it can be larger, as in panel B. We will see in the next section that $\hat{\pi}$ is the threshold level of expected profits below which the manager pays a positive wage and above which the wage is zero.

C. Properties of Optimal Relational Contracts

We now turn to properties of the optimal relational contract. We continue to focus on the relaxed problem that ignores the IC_W constraint. The next lemma shows that any optimal relational contract is sequentially optimal.

LEMMA 3: *Any optimal relational contract is sequentially optimal, that is, for any PPE payoff pair $(\pi, u(\pi))$, the associated continuation payoffs satisfy $u_s = u(\pi_s)$ and $u_n = u(\pi_n)$.*

Essentially, since the worker’s actions are publicly observable, it is not necessary to punish him by moving below the PPE frontier. This feature of our model is similar, for instance, to Spear and Srivastava (1987) and the first part of Levin (2003). In contrast, joint punishments are necessary in models with two-sided private information, such as Green and Porter (1984), Athey and Bagwell (2001), and the second part of Levin (2003).

Recall from Lemma 2 that payoffs on the frontier are sustained by pure actions. Lemma 3 then implies that the optimal relational contract does not involve any public randomization. In what follows we therefore refer to an optimal relational contract as one in which no public randomization device is used.

Next we can simplify and combine some of the constraints in Section IIIA. In particular, the next lemma will allow us to eliminate the shock and no-shock bonuses from the above constraints.

LEMMA 4: *For any optimal relational contract with payoffs $(\pi, u(\pi))$, there exists a set of actions and continuation payoffs supporting it such that (i) the bonuses satisfy $b_n(\pi) \geq b_s(\pi) = 0$ and (ii) the manager’s truth-telling constraint in a no-shock period TT_N is binding.*

Since it is less expensive for the manager to pay the worker in a no-shock period than in a shock period, it is natural that $b_n(\pi) \geq b_s(\pi)$. As a result, one can always replicate a PPE in which $b_s(\pi) > 0$ with an economically equivalent one in which the shock bonus is zero. To do so, one simply has to add $b_s(\pi)$ to the wage and subtract it from the no-shock bonus. Finally, the fact that TT_N is binding follows from the concavity of the PPE frontier $u(\pi)$. Essentially, if TT_N were not binding, one could always reduce π_n and increase π_s in such a way that π remains the same and all the relevant constraints continue to be satisfied. Since the PPE frontier is concave, however, such a change would make the worker better off.

The lemma allows us to eliminate $b_s(\pi)$ from the constraints in Section IIIA by setting it equal to zero. Furthermore, we can now eliminate a number of these constraints. For instance, it is immediate that if TT_N is binding, TT_S is satisfied. The next lemma shows that we can represent the PPE frontier by focusing on only four of the above constraints.

LEMMA 5: *The PPE frontier $u(\pi)$ is recursively defined by the following problem. For all $\pi \in [\underline{\pi}, \bar{\pi}]$,*

$$\begin{aligned} \pi + u(\pi) = \max_{e, w, \pi_s, \pi_n} & (1 - \delta)(y(e) - c(e)) \\ & + \theta\delta(\pi_s + u(\pi_s)) + (1 - \theta)\delta(\pi_n + u(\pi_n)) - (1 - \delta)\theta\alpha w \end{aligned}$$

such that

- (NN_w) $w \geq 0,$
- (SE_N) $\underline{\pi} \leq \pi_n \leq \bar{\pi},$
- (SE_S) $\underline{\pi} \leq \pi_s \leq \bar{\pi},$

and

$$(PK_M) \quad \pi = (1 - \delta)y(e) + \delta\pi_s - (1 - \delta)(1 + \theta\alpha)w.$$

Notice that there might be multiple functions $u(\pi)$ that solve this problem. This type of multiplicity is common in games of relational contracts (see, for instance, Baker, Gibbons, and Murphy 1994). When multiple solutions exist, it is immediate that the PPE frontier is given by the largest one.

In the next section we characterize the solution to this problem and show that it satisfies the IC_w constraint that we have ignored so far. The solution to the problem in the Lemma 5 therefore characterizes the optimal relational contracts for the full problem.

IV. The Optimal Relational Contract

In this section we characterize the optimal relational contract. We saw in the previous section that there is no loss of generality in setting the shock bonus equal to zero. We therefore now define an optimal relational contract to be a PPE that is not Pareto-dominated by any other PPE and in which $b_s = 0$. Our first proposition characterizes the optimal relational contract and shows that it is unique. In the proof of the proposition we solve the relaxed problem in Lemma 5 and then show that it satisfies the IC_w constraint that we ignored so far.

PROPOSITION 1: *For any level of expected profits π , there exists a unique optimal relational contract that gives the worker $u(\pi)$. Under the optimal relational contract:*

(i) *The no-shock bonus $b_n^*(\pi)$ is given by*

$$b_n^*(\pi) = \frac{\delta}{1 - \delta}(\bar{\pi} - \pi_s^*(\pi)) > 0 \quad \text{for all } \pi \in [\underline{\pi}, \bar{\pi}].$$

(ii) *If the firm is hit by a shock, the continuation profit $\pi_s^*(\pi)$ satisfies*

$$\pi_s^*(\underline{\pi}) = \underline{\pi} \text{ and } \pi_s^*(\pi) < \pi \quad \text{for all } \pi \in (\underline{\pi}, \bar{\pi}].$$

(iii) *If the firm is not hit by a shock, the continuation profit is given by*

$$\pi_s^*(\pi) = \bar{\pi} \quad \text{for all } \pi \in [\underline{\pi}, \bar{\pi}].$$

(iv) *Effort $e^*(\pi)$ is given by the unique effort level e that solves*

$$\frac{c'(e)}{y'(e)} = -u'(\pi) \quad \text{for all } \pi \in [\underline{\pi}, \bar{\pi}].$$

(v) *The wage is given by*

$$w^*(\pi) = \max \left[\frac{\hat{\pi} - \pi}{(1 - \delta)(1 + \alpha\theta)}, 0 \right] \quad \text{for all } \pi \in [\underline{\pi}, \bar{\pi}].$$

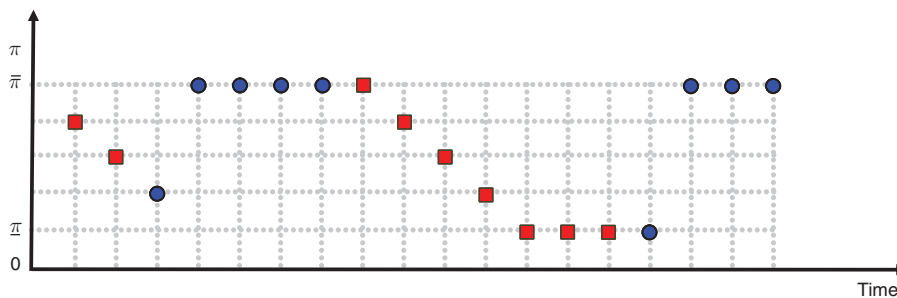


FIGURE 3. EVOLUTION OF EXPECTED PROFITS

The optimal relational contract reflects a balancing of incentives. In particular, the manager must give the worker an incentive to provide effort, while the worker must give the manager an incentive to make any promised payments. Part (i) shows that the manager motivates the worker to provide effort by promising him a bonus. The promise, however, is contingent on opportunity costs being low. The worker must therefore motivate the manager to act truthfully.

To motivate the manager to act truthfully, the worker punishes her if she does not pay the bonus and rewards her if she does. In particular, part (ii) shows that if the manager does not pay the bonus, expected profits will be strictly lower next period, unless they are already at their lower bound $\underline{\pi}$, in which case they stay there. In contrast, part (iii) shows that if the manager does pay the bonus, expected profits immediately jump to their upper bound $\bar{\pi}$ in the next period. Expected profits therefore cycle indefinitely, and the relationship never terminates. These cycles differ in length depending on the number of consecutive shock periods the firm experiences. They all, however, follow the same pattern in which downturns are gradual and recoveries instantaneous. These dynamics are illustrated in Figure 3, which plots expected profits for an arbitrary sequence of shock periods—indicated by lighter squares—and no-shock periods—indicated by darker dots.

To understand why downturns are gradual and recoveries are instantaneous, recall that joint surplus $\pi + u(\pi)$ is increasing in expected profits. Rewarding the manager for paying the bonus is therefore both good for her incentives to act truthfully and efficiency enhancing. As a result, it is optimal for expected profits to jump to their upper bound if the manager pays the bonus. In contrast, punishing the manager for not paying the bonus involves a destruction of joint surplus. In principle, the worker could punish the manager for not paying the bonus by insisting that expected profits plummet to $\underline{\pi}$ in the next period. One way to do so would be to terminate the relationship. As discussed after Lemma 3, however, termination is not optimal in our setting since the public observability of the worker's actions makes joint punishments unnecessary. Another way to force expected profits to $\underline{\pi}$ would be to reduce effort significantly for a number of periods without, however, terminating the relationship. The dynamics would then be reminiscent of those in Green and Porter (1984) in which the parties alternate between cooperation and noncooperation phases. Because of the concavity of the production function, however, such a punishment is not optimal in our setting. Instead, the optimal punishment involves changes to the bonus, effort, and wages that lead to a gradual reduction in expected profits.

Specifically, part (i) shows that the optimal punishment involves an increase in the bonus that the manager has to pay the worker in the next period. Since the bonus has to be paid only if opportunity costs turn out to be low, this part of the punishment is efficient. But since the opportunity costs are observed only by the manager, the optimal punishment must also involve changes in the wage, effort, or both.

The last two parts of the proposition show that if expected profits are high, the optimal punishment involves a reduction in effort but no change in the wage; and if expected profits are low, the optimal punishment involves an increase in the wage but no change in effort. To see this formally, recall from Section IIIB that $\hat{\pi}$ is the critical level of expected profits below which the derivative of the PPE frontier is at its upper bound. Part (iv) then implies that effort is the same for all $\pi \leq \hat{\pi}$ and increasing in expected profits for all $\pi > \hat{\pi}$. At the same time, part (v) implies that wages are decreasing in expected profits for all $\pi \leq \hat{\pi}$ and zero for all $\pi > \hat{\pi}$. Essentially, because of the concavity of the production function, there is a threshold level of profits above which it is more efficient to punish the manager through a reduction in effort and below which it is more efficient to do so through an increase in the wage.

To see this more clearly, consider two ways in which expected profits can be reduced by some $\varepsilon > 0$. One way to do so is to reduce effort by $\varepsilon/y'(e)$ and the other is to increase wages by $\varepsilon/(1 + \alpha\theta)$. The reduction in effort increases the worker's expected payoff by $\varepsilon c'(e)/y'(e)$, while the increase in wages increases it by $\varepsilon/(1 + \alpha\theta)$. Recall now from Section IIIB that the effort level \hat{e} that is associated with expected profits $\hat{\pi}$ is defined by $c'(\hat{e})/y'(\hat{e}) = 1/(1 + \alpha\theta)$. For expected profits above $\hat{\pi}$ it is therefore more efficient to punish the manager through a reduction in effort, and for expected profits below $\hat{\pi}$ it is more efficient to do so through an increase in the wage.

To illustrate the evolution of bonuses, effort, and wages over time, suppose that expected profits are at their upper bound $\bar{\pi}$ and that the firm is then hit by shocks in a large number of consecutive periods. The resulting conflict goes through three distinct phases, which are illustrated in Figure 4. As in Figure 3, lighter squares indicate shock periods, and darker dots indicate no-shock periods.

In the initial phase of the conflict, the bonus is increasing, and effort is decreasing. Wages, however, stay constant at zero. Once expected profits fall below $\hat{\pi}$, the conflict enters its second phase. During this phase the bonus is still increasing. Wages, however, are now also increasing, while effort is constant at $\hat{e} > 0$. Eventually, expected profits hit their lower bound, at which point the conflict enters its final phase. During this phase, the bonus and the wage stay constant at their maximized levels, and effort stays constant at \hat{e} . This final phase of the conflict continues until the parties reach a period in which the firm is not hit by a shock. In that period the manager finally pays the promised bonus, and expected profits return to their upper bound $\bar{\pi}$.

The prediction that the firm sometimes does not pay any wages is at odds with the fact that most workers have a contracted wage which has to be paid except in the case of bankruptcy. One way to account for wages would be to allow for the worker to be risk averse, in which case the manager would find it optimal to pay him some amount every period. Alternatively, one could assume that the firm has to pay the worker a minimum wage every period. Such a minimum wage would not affect the key features of the optimal relational contract and the dynamics that we

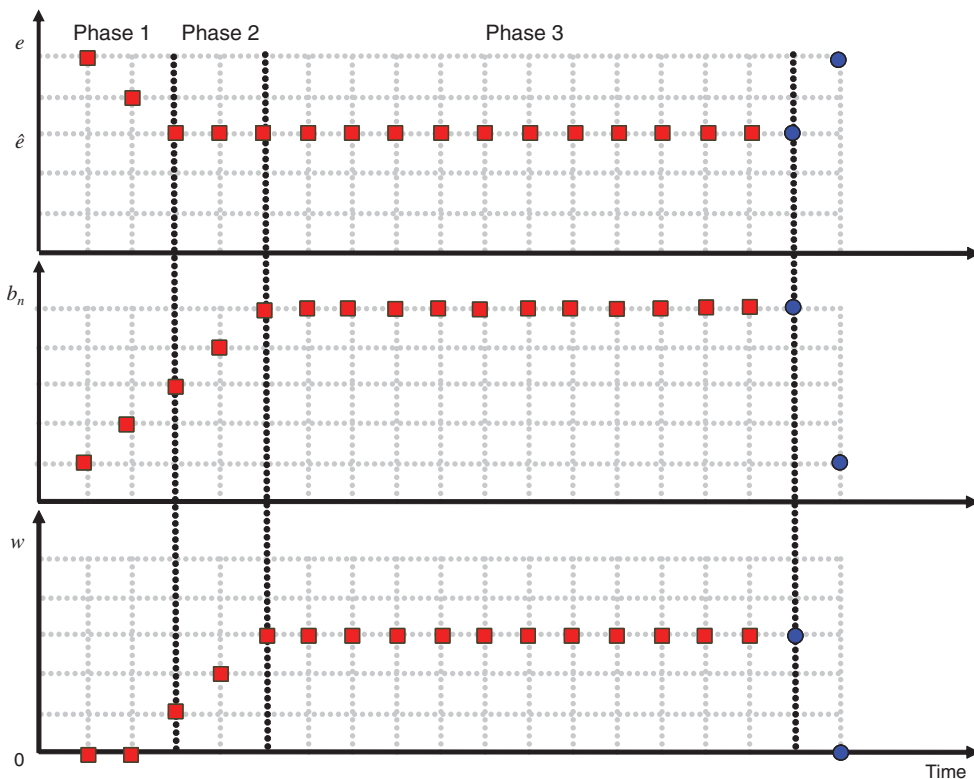


FIGURE 4. EVOLUTION OF EFFORT, BONUSES, AND WAGES

described above. Another prediction that is worth discussing is that the manager makes the largest payments to the worker at the end of a severe conflict. This prediction depends crucially on the assumption that the firm is not liquidity constrained. We will see in the next section that if the firm is liquidity constrained, the manager may be forced to spread the payment over multiple periods, making the changes in the predicted payments less stark.

Finally, changes in the underlying parameters, such as the size and probability of the shock α and θ , the outside options u and $\underline{\pi}$, and the discount factor δ , do not affect the key features of the optimal relational contract and the dynamics that we described above. As one would expect, however, such changes do affect the set of payoffs that can be sustained as PPEs. In particular, it can be shown that the PPE frontier $u(\pi)$ and the maximum sustainable profits $\bar{\pi}$ are decreasing in α , θ , u , and $\underline{\pi}$ and increasing in δ . Other things equal, the manager and the worker are therefore better off the smaller and less frequent the shocks are, the lower the outside options are, and the more patient the parties are.

V. The Effects of Liquidity Constraints

The Lincoln Electric case we discussed in the Introduction suggests that liquidity constraints can have significant effects on managers' ability to manage conflicts. In this section we explore this issue by allowing for the firm to be liquidity constrained.

Specifically, we now assume that if the firm realizes output $y(e)$ and is not hit by a shock, the manager can pay the worker at most $(1 + m)y(e)$, where the parameter $m \geq 0$ captures the extent to which the firm is liquidity constrained. Liquidity constraints make the PPE frontier nondifferentiable and, thus, substantially complicate the characterization of the optimal relational contract. To make the analysis more tractable, we now assume that the size of the shock α is equal to infinity. An immediate implication of this assumption is that wages and the shock bonus are always equal to zero. The liquidity constraint is therefore given by

$$(LC) \quad b_n \leq (1 + m)y(e).$$

Finally, we assume that $(1 + m)\underline{\pi}/\delta$ is strictly smaller than the maximal expected profits if the firm is not liquidity constrained. If this condition did not hold, the liquidity constraint LC would never bind. We can now establish the following lemma.

LEMMA 6: *There exist critical levels of expected profits $\pi_0 \leq \pi_1 \leq \pi_2 < \bar{\pi}$ such that:*

- (i) *if $\pi \in [\underline{\pi}, \pi_0]$, then $u(\pi)$ is supported by randomization between $(\underline{\pi}, \underline{u})$ and $(\pi_0, u(\pi_0))$,*
- (ii) *if $\pi \in [\pi_1, \bar{\pi}]$, then the self-enforcing constraint $\pi_n \leq \bar{\pi}$ is binding, and*
- (iii) *if $\pi \in [\pi_0, \pi_2)$, then the liquidity constraint $b_n \leq (1 + m)y(e)$ is binding.*

Part (i) shows that, in contrast to the model without liquidity constraints, termination can now be part of the optimal relational contract. Specifically, for any $\pi \in [\underline{\pi}, \pi_0]$, the manager and the worker publicly randomize between terminating their relationship and playing the strategies that deliver expected payoffs π_0 and $u(\pi_0)$. One way to implement termination is for the manager to always offer a zero wage and no bonus and for the worker to always turn down this offer; moreover, in case either party deviates from these actions, the worker always provides zero effort, and the manager never pays a bonus. The relationship therefore terminates eventually as long as $\pi_0 > \underline{\pi}$. A pair of sufficient conditions for $\pi_0 > \underline{\pi}$ is given by $m < \theta/(1 - \theta)$ and

$$\underline{u} > \frac{(1 - \theta)(1 + m)}{\theta - (1 - \theta)m} \left(1 - \frac{c'(\underline{e})}{y'(\underline{e})} \right) \underline{\pi} - c(\underline{e}),$$

where \underline{e} is the effort level for which $y(\underline{e}) = \underline{\pi}$. In the online Appendix we show that these conditions ensure that the joint surplus at $\underline{\pi}$ is larger under termination than if the manager and the worker were to continue their relationship. As a result, termination must occur. Notice that these conditions are more likely to be satisfied the smaller m , suggesting that termination is more likely to occur the more liquidity constrained the firm is.

Parts (ii) and (iii) show that to the right of π_0 there are three regions. If expected profits are sufficiently high, the liquidity constraint is not binding. The manager is then able to pay a sufficiently large bonus for expected profits to return to $\bar{\pi}$ after a no-shock period. If, in contrast, expected profits are sufficiently low, the self-enforcing constraint

is not binding, which implies that expected profits do not return to $\bar{\pi}$ after a no-shock period. This occurs because effort and output are too low for the manager to be able to pay a sufficiently large bonus. Finally, for intermediate values of expected profits, both the liquidity constraint and the self-enforcing constraint are binding. We will see below that in this region, a reduction in expected profits is associated with an increase in effort. A pair of sufficient conditions for the intermediate region to exist is given by

$$(1 + m)^2(1 - \theta)\theta < m < \theta/(1 - \theta).$$

In the online Appendix we derive these conditions by contradiction. Specifically, suppose that the intermediate region does not exist. We can then show that the payoff frontier has a kink at the boundary between the left and the right region. We can also show, however, that under the above conditions the payoff frontier must be differentiable. Since this is a contradiction, the middle region must exist.

We can now state our next proposition, which characterizes the optimal relational contract when the firm is liquidity constrained.

PROPOSITION 2: *For any level of expected profits π , there exists a unique optimal relational contract that gives the worker $u(\pi)$. Under the optimal relational contract:*

(i) *The no-shock bonus $b_n^*(\pi)$ is given by*

$$b_n^*(\pi) = \begin{cases} (1 + m)y(e^*(\pi)) > 0 & \text{for all } \pi \in [\pi_0, \pi_2) \text{ and} \\ \frac{\delta}{1 - \delta}(\bar{\pi} - \pi_s^*(\pi)) > 0 & \text{for all } \pi \in [\pi_2, \bar{\pi}]. \end{cases}$$

(ii) *If the firm is hit by a shock, the continuation profit $\pi_s^*(\pi)$ satisfies*

$$\pi_s^*(\pi_0) = \underline{\pi} \text{ and } \pi_s^*(\pi) < \pi \quad \text{for all } \pi \in [\pi_0, \bar{\pi}].$$

(iii) *If the firm is not hit by a shock, the continuation profit $\pi_n^*(\pi)$ is given by*

$$\pi_n^*(\pi) = \begin{cases} [\pi + (1 - \delta)my(e^*(\pi))]/\delta & \text{for all } \pi \in [\pi_0, \pi_1) \text{ and} \\ \bar{\pi} & \text{for all } \pi \in [\pi_1, \bar{\pi}]. \end{cases}$$

(iv) *Effort is given by the unique effort level $e^*(\pi)$ that solves*

$$\frac{c'(e)}{y'(e)} = \begin{cases} -u'_+(\pi) + (1 + m)(1 - \theta)(1 + u'_+(\pi_n^*(\pi))) & \text{for all } \pi \in [\pi_0, \pi_1), \\ -u'(\pi) & \text{for all } \pi \in [\pi_2, \bar{\pi}], \end{cases}$$

and

$$y(e) = (\delta\bar{\pi} - \pi)/((1 - \delta)m) \quad \text{for all } \pi \in [\pi_1, \pi_2),$$

where $u'_+(\cdot)$ denotes the right derivative.

The proposition shows that most of the features of the optimal relational contract are not affected by liquidity constraints. In particular, part (i) shows that the manager still motivates the worker by promising him a strictly positive bonus. Notice, however, that when the liquidity constraint is binding, that is, $\pi \in [\pi_0, \pi_2)$, there is a limit to the size of the bonus. In this region, the manager would like to pay a larger bonus but is constrained to paying $b_n^*(\pi) = (1 + m)y(e^*(\pi))$.

Part (ii) shows that, as in the case without liquidity constraints, the worker punishes the manager for not paying bonuses by gradually reducing expected profits. While downturns are still gradual, however, part (iii) shows that recoveries may no longer be instantaneous. Specifically, when $\pi \in [\pi_0, \pi_1)$, $\pi_n^*(\pi)$ is strictly less than $\bar{\pi}$, even though the manager is paying the largest possible bonus. When $\pi \in [\pi_1, \pi_2)$ this bonus is sufficient to compensate the worker for letting expected profits return to $\bar{\pi}$. When $\pi \in [\pi_0, \pi_1)$, however, the largest possible bonus is too small to compensate the worker. The manager then needs to spread the bonus payments over multiple periods. Liquidity constraints therefore slow down recoveries from sufficiently severe downturns.

Together with the Lemma 6, part (ii) also implies that the relationship terminates if $\pi_0 > \underline{\pi}$ and the firm is hit by shocks in sufficiently many consecutive periods. The reason is that after a sufficiently severe downturn the manager's reward for paying a bonus is limited since it then takes multiple periods for expected profits to return to their upper bound. To ensure that the manager stays truthful, the worker therefore has to increase the punishment for the manager not paying the bonus. Since expected profits are already small, the only way to do so is to increase the threat of termination.

Finally, part (iv) shows how liquidity constraints affect effort provision. When the liquidity constraint is not binding, that is, $\pi \in [\pi_2, \bar{\pi}]$, the expression that determines effort is the same as in the model without liquidity constraints. In particular, the ratio of marginal effort costs to marginal output is again equal to the negative of the slope of the payoff frontier. In contrast, when the liquidity constraint is binding, that is, $\pi \in [\pi_0, \pi_2)$, the ratio of marginal effort costs to marginal output is always strictly larger than the negative of the slope of the payoff frontier. The reason is that an increase in effort now has the additional benefit of relaxing the liquidity constraint. If $\pi \in [\pi_0, \pi_1)$, this additional benefit is captured by the second term on the right-hand side of the expression in part (iv). And if $\pi \in [\pi_1, \pi_2)$, effort is raised just enough for expected profits to return to $\bar{\pi}$ following a no-shock period. Notice that in this region effort is decreasing in expected profits. The worker, therefore, responds to a reduction in expected profits by providing more effort rather than less. Essentially, the worker understands that providing more effort relaxes the firm's liquidity constraint which, in turn, allows the manager to pay him a larger bonus if the firm is not hit by another shock. As discussed in the Introduction, this reasoning is broadly consistent with the experience at Lincoln Electric.

In summary, liquidity constraints limit the manager's ability to manage conflicts, which slows down recoveries and can lead to termination. Liquidity constraints, however, can also induce the worker to respond to a conflict by providing more effort rather than less.

VI. Discussion

In this section we revisit key features and assumptions of our model and examine them in more detail. We focus on our main model without liquidity constraints.

A. *The Failure to Achieve First-Best*

We show in online Appendix C (Proposition C1) that the Folk Theorem holds in our setting. Specifically, we show that as the discount factor δ goes to one, the limit set of the PPE payoff contains the interior of the set of feasible payoffs. Joint surplus therefore converges towards first-best as the parties become increasingly patient. It is important to note, however, that as long as the discount factor δ is strictly less than one, joint surplus is strictly less than first-best. For any $\delta < 1$ the optimal relational contract is, therefore, inefficient. This is in line with related repeated games such as Hertel (2004) in which first-best also cannot be achieved. In contrast, first-best can be achieved, for instance, in Athey and Bagwell (2001).

The reason for the parties' inability to achieve first-best is that the worker can never be sure that opportunity costs are low. The fact that the worker can never be sure that opportunity costs are high, in contrast, does not matter for the parties' inability to achieve first-best. To see this, suppose that whenever the firm is not hit by a shock, there is some probability $p \in [0, 1)$ with which it becomes publicly known that the firm's opportunity costs are low. And whenever the firm is hit by a shock, there is some probability $q \in [0, 1)$ with which it becomes publicly known that the firm's opportunity costs are high. If $p = q = 0$, this model is the same as our main model. And if either p or q were equal to one, the state would be publicly observed and there would be no need for the manager to be punished on the equilibrium path. We discuss this public information benchmark in the next section. In online Appendix C (Proposition C2) we show that in the setting in which $p \in [0, 1)$ and $q \in [0, 1)$, first-best can be achieved for sufficiently high discount factors if and only if $p > 0$. Essentially, when $p > 0$, the manager does not pay the worker when the firm is hit by a shock but promises him a larger bonus in the next period in which it is publicly observed that the firm's opportunity costs are low. Since the occurrence of such an event is publicly observable, the manager's promise is credible and first-best is feasible.

Firms that ask their workers to accept cuts to their compensation often open their books to prove that those cuts really are necessary (see, for instance, the Introduction and Engmaier and Segal 2011). The above argument suggests that firms should not only open their books during hard times, in the hope of avoiding worker punishments. Instead, it may be even more important for firms to keep their books open during good times, so as to make punishments less costly.

B. *Benchmarks: Public Information and Long-Term Contracts*

The first benchmark we examine is one in which shocks are publicly observed. In online Appendix C (Proposition C3) we examine this case and characterize the PPE payoff set. For every payoff pair on the PPE frontier we then characterize the optimal relational contract supporting it. As in our main model, expected profits, effort,

and joint surplus jump to their upper bounds following a no-shock period. Because of the public observability of the opportunity costs, however, shocks no longer lead to a reduction in expected profits. Instead, following a shock period, expected profits, effort, and joint surplus remain unchanged. They therefore reach their highest achievable levels with probability one and then stay there forever. Finally, if the manager and the worker are patient enough, those highest achievable levels are equal to first-best. The evolution of the relationship between the manager and the worker therefore depends crucially on whether shocks are publicly observed.

The second benchmark we examine is one in which the manager can commit to a long-term contract. Suppose that in any period t the manager first observes the state $\Theta_t \in \{n, s\}$ and then makes an announcement $m_t \in \{n, s\}$ about the state. Suppose also that before the first period, the manager can commit to a contract that, for any period t , maps her announcements (m_1, m_2, \dots, m_t) into the bonus b_t that she has to pay the worker at the end of period t .

A long-term contract does not allow the parties to achieve first-best. It does, however, allow them to approximate first-best. To see this, let $\tau(t)$ denote the number of consecutive periods immediately preceding t in which the manager did not pay the worker. Now consider a contract with three features. First, the contract asks the worker to provide first-best effort in all periods. If the worker ever does not provide first-best effort, the manager will never again pay him. Second, the contract specifies that if, in period t , the manager announces that the firm has not been hit by a shock, she pays the worker a bonus

$$b_t(\tau(t)) = \left(1 + \frac{1}{\delta} + \frac{1}{\delta^2} + \dots + \frac{1}{\delta^{\tau(t)}}\right)(\underline{u} + c(e^{FB})).$$

And third, the contract specifies the maximum number of consecutive periods $T \geq 1$ that the manager can go without paying the worker the bonus. In particular, if, in period t , the manager announces that the firm has been hit by a shock and if $\tau(t) < T$, the manager does not have to pay the worker. If, however, $\tau(t) = T$, the manager has to pay the worker a bonus $b_t(T)$.

In online Appendix C (Proposition C4) we show that under such a contract, the worker always provides first-best effort, and the manager always announces the state truthfully. Essentially, under this contract the manager has to pay the worker $(\underline{u} + c(e^{FB}))$ per period, independent of her announcements. By lying about the state, the manager can therefore affect the timing of payments but not their net present value.

This contract does not achieve first-best since it induces inefficient payment whenever the firm is hit by shocks in T consecutive periods. By agreeing to a large T , however, the parties can come arbitrarily close to achieving first-best. The evolution of the relationship between the manager and the worker therefore depends crucially on whether the manager is able to commit to a long-term contract. And as we saw above, it also depends on whether shocks are privately observed.

VII. Conclusions

In a well-known article in *The New Yorker*, Stewart (1993) describes the upheavals at the investment bank Credit Suisse First Boston (CSFB) after consecutive

years of disappointing bonus payments. Problems started in 1991 when traders demanded that management pay them a higher bonus. Management, however, stood firm, insisting that a higher bonus was not justified because of the need to “build capital” (Stewart 1993, p. 37). To appease the traders, management then simply “promised that 1992 would be different—that salaries and bonuses would again be competitive” (Stewart 1993, p. 37). Traders were forthcoming in expressing their disappointment, but their retaliations were limited. The traders’ behavior changed the following year, however, when bonus payments were once again below expectations. This time “many traders seemed to drag their heels, further depressing the firm’s earnings” and “defections [...] increased as soon as First Boston actually began paying bonuses” (Stewart 1993, pp. 37–38). This response forced management to adapt its compensation policy by formally committing to “guaranteed pay raises,” in some cases as much as 100 percent (Stewart 1993, p. 38).

At the heart of the conflict at CSFB was uncertainty, and possibly private information, about the opportunity costs of bonus payments. In particular, while there was no disagreement about the traders’ performance, there was disagreement about the extent to which bonus payments should be contingent on the need to “build capital.” The aim of this article was to explore the conflicts that arise in such a setting. In our model, it is optimal for the manager to make payments contingent on their opportunity costs, even though this makes conflicts inevitable. As in the CSFB example, the manager responds to such conflicts by adapting compensation to their duration, moving from the informal—promising that 1992 will be different—to the formal—committing to guaranteed pay raises. Because the manager responds to a conflict by changing the compensation she offers the worker, conflicts evolve gradually. This is again illustrated in the CSFB example in which traders did not switch from cooperation to punishment abruptly. Instead, the relationship deteriorated gradually in response to repeated disagreements about bonus pay. Finally, in our main model, expected profits cycle indefinitely. The relationship between the manager and the worker therefore never terminates, nor does it reach a steady state. This is in contrast to the CSFB example where many traders did leave. Termination, however, can also arise in our setting once we allow for the firm to be liquidity constrained.

To discuss the empirical implications and testability of our model, it is useful to note that the basic structure of the stage game is closely related to a “trust game.” In a standard trust game, the “proposer” first decides on the size of a monetary gift that he makes to the “responder.” The gift is then increased by some amount after which the responder decides how much to give back to the proposer. One can therefore view our model as an infinitely repeated trust game in which the responder faces shocks to the costs of giving back. There is an extensive literature in experimental economics that examines trust games. This suggests that one could test our model in a laboratory setting. Two predictions, in particular, are clear cut. First, the evolution of trust—as measured by the size of the gift—depends crucially on whether shocks are publicly observed. If shocks are publicly observed, trust increases over time until it tops out at some level. If shocks are instead privately observed, trust evolves through booms and busts. Second, the long-term prospects of a relationship depend on whether the responder is liquidity constrained. If the responder is not liquidity constrained, the relationship continues forever. But if she is liquidity constrained, it is certain to terminate eventually.

We have cast our model in the context of an employment relationship. The main ingredients of the model—repeated interaction, limited commitment, and inefficient transfers—are also relevant in many other economic settings. One example is the lending relationship between an entrepreneur and an investor who are not able to commit to long-term contracts. The entrepreneur can have private information about her marginal value of money, and the investor can adjust his future financing terms based on the payment history of the entrepreneur. Another example is that of long-term and informal supplier relationships in which buyers face shocks to their ability to pay their suppliers. In 1995, for instance, Continental Airlines was close to bankruptcy, and its “most pressing need was to shore up its cash position. The airline [...] was only able to make its January 1995 payroll when [its CEO] Bethune successfully begged Boeing to return cash deposits on aircraft whose delivery he had deferred” (Frank 2009). A final example involves the informal insurance relationships among farmers in developing countries. There is some evidence that the farmers’ income is private information (see, for example, Kinnan 2011). While most of the literature has focused on moral hazard and insurance issues separately, our model suggests that these issues are related, since insurance decisions affect future production choices.

REFERENCES

- Abdulkadiroğlu, Atila, and Kyle Bagwell.** 2013. “Trust, Reciprocity, and Favors in Cooperative Relationships.” *American Economic Journal: Microeconomics* 5 (2): 213–59.
- Abreu, Dilip, David Pearce, and Ennio Stacchetti.** 1990. “Toward a Theory of Discounted Repeated Games with Imperfect Monitoring.” *Econometrica* 58 (5): 1041–63.
- Athey, Susan, and Kyle Bagwell.** 2001. “Optimal Collusion with Private Information.” *RAND Journal of Economics* 32 (3): 428–65.
- Athey, Susan, and Kyle Bagwell.** 2008. “Collusion with Persistent Cost Shocks.” *Econometrica* 76 (3): 493–540.
- Athey, Susan, Kyle Bagwell, and Chris Sanchirico.** 2004. “Collusion and Price Rigidity.” *Review of Economic Studies* 71 (2): 317–49.
- Baker, George, Robert Gibbons, and Kevin J. Murphy.** 1994. “Subjective Performance Measures in Optimal Incentive Contracts.” *Quarterly Journal of Economics* 109 (4): 1125–56.
- Baker, George, Robert Gibbons, and Kevin J. Murphy.** 2002. “Relational Contracts and the Theory of the Firm.” *Quarterly Journal of Economics* 117 (1): 39–84.
- Biais, Bruno, Thomas Mariotti, Guillaume Plantin, and Jean-Charles Rochet.** 2007. “Dynamic Security Design: Convergence to Continuous Time and Asset Pricing Implications.” *Review of Economic Studies* 74 (2): 345–90.
- Chassang, Sylvain.** 2010. “Building Routines: Learning, Cooperation, and the Dynamics of Incomplete Relational Contracts.” *American Economic Review* 100 (1): 448–65.
- Che, Yeon-Koo, and Seung-Weon Yoo.** 2001. “Optimal Incentives for Teams.” *American Economic Review* 91 (3): 525–41.
- Clementi, Gian Luca, and Hugo A. Hopenhayn.** 2006. “A Theory of Financing Constraints and Firm Dynamics.” *Quarterly Journal of Economics* 121 (1): 229–65.
- DeMarzo, Peter M., and Michael J. Fishman.** 2007. “Optimal Long-Term Financial Contracting.” *Review of Financial Studies* 20 (6): 2079–128.
- DeMarzo, Peter M., and Yuliy Sannikov.** 2006. “Optimal Security Design and Dynamic Capital Structure in a Continuous-Time Agency Model.” *Journal of Finance* 61 (6): 2681–724.
- Englmaier, Florian, and Carmit Segal.** 2011. “Cooperation and Conflict in Organizations.” Unpublished.
- Fong, Yuk-fai, and Jin Li.** 2010. “Relational Contracts, Efficiency Wages, and Employment Dynamics.” Unpublished.
- Frank, Douglas.** 2009. “Continental Airlines: The Go Forward Plan.” INSEAD Case No. 10/2009–5565.

- Fuchs, William.** 2007. "Contracting with Repeated Moral Hazard and Private Evaluations." *American Economic Review* 97 (4): 1432–48.
- Green, Edward J., and Robert H. Porter.** 1984. "Noncooperative Collusion under Imperfect Price Information." *Econometrica* 52 (1): 87–100.
- Halac, Marina.** 2012. "Relational Contracts and the Value of Relationships." *American Economic Review* 102 (2): 750–79.
- Hastings, Donald.** 1999. "Lincoln Electric's Harsh Lessons from International Expansion." *Harvard Business Review* 77 (3): 162–78.
- Hauser, Christine, and Hugo Hopenhayn.** 2008. "Trading Favors: Optimal Exchange and Forgiveness." Unpublished.
- Hertel, Johanna.** 2004. "Efficient and Sustainable Risk Sharing with Adverse Selection." Unpublished.
- Kinnan, Cynthia.** 2011. "Distinguishing Barriers to Insurance in Thai Villages." Unpublished.
- Kocherlakota, Narayana R.** 1996. "Implications of Efficient Risk Sharing without Commitment." *Review of Economic Studies* 63 (4): 595–609.
- Levin, Jonathan.** 2002. "Multilateral Contracting and the Employment Relationship." *Quarterly Journal of Economics* 117 (3): 1075–103.
- Levin, Jonathan.** 2003. "Relational Incentive Contracts." *American Economic Review* 93 (3): 835–57.
- Ligon, Ethan, Jonathan P. Thomas, and Tim Worrall.** 2002. "Informal Insurance Arrangements with Limited Commitment: Theory and Evidence from Village Economies." *Review of Economic Studies* 69 (1): 209–44.
- MacLeod, W. Bentley.** 2007. "Reputations, Relationships, and Contract Enforcement." *Journal of Economic Literature* 45 (3): 595–628.
- MacLeod, W. Bentley, and James M. Malcomson.** 1989. "Implicit Contracts, Incentive Compatibility, and Involuntary Unemployment." *Econometrica* 57 (2): 447–80.
- MacLeod, W. Bentley, and James M. Malcomson.** 1998. "Motivation and Markets." *American Economic Review* 88 (3): 388–411.
- Mailath, George, and Larry Samuelson.** 2006. *Repeated Games and Reputations*. Oxford: Oxford University Press.
- Malcomson, James.** 2013. "Relational Incentive Contracts." In *The Handbook of Organizational Economics*, edited by Robert Gibbons and John Roberts, 1014–65. Princeton: Princeton University Press.
- Möbius, Markus.** 2001. "Trading Favors." Unpublished.
- Mukherjee, Arijit, and Luis Vasconcelos.** 2011. "Optimal Job Design in the Presence of Implicit Contracts." *RAND Journal of Economics* 42 (1): 44–69.
- Padro i Miquel, Gerard, and Pierre Yared.** 2012. "The Political Economy of Indirect Control." *Quarterly Journal of Economics* 127 (2): 947–1015.
- Rayo, Luis.** 2007. "Relational Incentives and Moral Hazard in Teams." *Review of Economic Studies* 74 (3): 937–63.
- Samuelson, Larry.** 2006. "The Economics of Relationships." In *Advances in Economics and Econometrics: Theory and Applications, Ninth World Congress*. Econometric Society Monographs, No. 41. Volume 1, edited by Richard Blundell, Whitney K. Newey, and Torsten Persson, 136–85. New York: Cambridge University Press.
- Spear, Stephen E., and Sanjay Srivastava.** 1987. "On Repeated Moral Hazard with Discounting." *Review of Economic Studies* 54 (4): 599–617.
- Stewart, James.** 1993. "Taking the Dare." *The New Yorker* 69 (23): 34–9.
- Thomas, Jonathan, and Tim Worrall.** 1990. "Income Fluctuation and Asymmetric Information: An Example of a Repeated Principal-Agent Problem." *Journal of Economic Theory* 51 (2): 367–90.
- Thomas, Jonathan, and Tim Worrall.** 2010. "Dynamic Relational Contracts under Limited Liability." Unpublished.
- Watson, Joel.** 1999. "Starting Small and Renegotiation." *Journal of Economic Theory* 85 (1): 52–90.
- Watson, Joel.** 2002. "Starting Small and Commitment." *Games and Economic Behavior* 38 (1): 176–99.
- Yang, Huanxing.** 2013. "Nonstationary Relational Contracts." Unpublished.
- Yared, Pierre.** 2010. "A Dynamic Theory of War and Peace." *Journal of Economic Theory* 145 (5): 1921–50.